# The application of linear programming to farm management: a study of a central Iowa farm 

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THE APPLICATION OF LINEAR PROGRAMMING TO FARM

MANAGEMENT: A STUDY OF A CENTRAL IOWA FARM

by<br>Malcolm David Bale

A Thesis Submitted to the Graduate Faculty in Partial Fulfillment of The Requirements for the Degree of MASTER OF SCIENCE Major Subject: Economics

Signatures have been redacted for privacy

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## I. INTRODUCTION

## A. Farm Management

The successful commercial farmer today is an intelligent, wellinformed businessman oriented to and responding to commercial market situations in such a manner as to maximize profits. ${ }^{1}$ In this context farm production is only partly dependent on natural resources and technology, and is equally or more dependent on economic variables such as prices, costs, and producers' income.

With the growing emphasis on economic aspects of farming together with the trend towards greater capital intensity on farms, farm management has become increasingly complex. The restriction on the magnitude of profits has become less one of aquaintance with farm practices and more one of properly fitting all production alternatives into an integrated plan consistent with resource supplies and market prices. In this setting farm management may be defined as those decisions that affect the profitability of the farm business. Management concerns the process of gathering information, of interpreting it, of making decisions, and of accepting the consequences of decisions made and acted upon in a previous time period. Accordingly, successful farm management requires that the manager have the ability to make the "right" decisions in the sense that, ex-post, they are the most profitable ones.

[^0]The management process is not mechanistic but very much a human phenomenon. It is an aggregation of interacting human goals, beliefs, values, experiences, and expectations, constrainedby exogenous physical, social, economic, and temporal phenomena. The management process is so complex, in fact, that social scientists are only now attempting to systematize it for the purpose of simulating it in mechanistic models. This approach is called a "Behavioral Theory of the Firm" and has been described by Cyert and March (7) and applied by Shechter (36). Prior to this development the management process had only been studied in terms of its visible effects. Social scientists studied the results of management and pinned them to some objective scale of success-failure, often a profit scale. A great deal of research has been done in which organizational or operational goals were assumed, and then a set of managerial decisions deduced that would optimize the managers attainment of the assumed goal. Production economics has become a discipline of economics specializing in the search for production and organizational optima.

By now we are aware of the fact that goals other than profit maximization enter into decisions made by managers. We shall therefore redefine "right" decisions as used on page 1 to include all decisions resulting in the maximization of a farmer's objectives, one of which is to make a profit on his operation. Our definition of "successful management" now becomes broadened to include non-profit objectives as we in fact find in reality.

Implicit in the foregoing discussion is the fact that the need for management grows out of change and the inability to predict the future
with certainty. The dynamic nature of the economy in which agriculture operates necessitates continual revision of farm plans as more information becomes available. As Heady and Jensen state, "If yields did not vary and prices fluctuate from year to year, a farmer's first decision might well be his last. He would devise a single and final plan for the farm based on realizing the most profit from his land and other resources in the pleasant expectation that this sameeconomic situation might last for years" (21, p. 7).

Skillful management not only involves effective organization of short run plans but the ability to plan long run firm growth and development. In the long run a firm has more flexibility and more alternatives available to it as all resources become variable.

Some of the more general decisions affecting profitability in farming might be: 1) What size should a farm be and what land tenure system is most suitable? 2) What enterprises should be pursued and at what level? 3) At what time should farm products be sold or farm inputs purchased? 4) Should extra labor be hired and/or extra capital borrowed? What quantity of each should be employed and how should they be allocated between enterprises? 5) What types and rates of fertilizer should be applied? 6) What equipment is it profitable to purchase and how much custom work should be hired?

As is obvious from the above list, farm planning, if it incorporates a11 relevant farming practices, investment alternatives, and scarcity of resources, is a complicated process. Extension personnel and farmers
seldom have the skill to consider fully all appropriate alternatives in formulating farm plans. A manager may be so involved with the everyday affairs of his firm that he cannot "step back" and view the farm as a whole to plan its future development. As a consequence a "piece-meal" approach to farm business decisions has been the norm. This approach ignores the direct or indirect effects that a given change in one part of the farm has on other parts, and as such may be severely limiting.

Linear programming as applied to farm management offers the opportunity to consider simultaneously all possible farming activities and, mindful of resource restraints, give a profit maximizing farm plan. In this study we utilize the technique of linear programming in analyzing the operations of a particular farm-firm.

## B. Definitions and Concepts

The terminology of even that small part of the literature of economics relating to production in agriculture is highly volatile. The various interpretations to which certain words are open leads to considerable confusion. Already in this thesis words and phrases have been used without adequate explanation. Accordingly some explicit definitions of certain terms and concepts used in this study will now be given.

1. The farm-firm

We will consider a firm to be a business entity whose primary purpose is the creation (or increase) of monetary profit. A farm is a set of resources and activities functionally concerned with the creation of
agricultural products. Thus a farm-firm by the above definitions is a business entity primarily concerned with creating monetary profit primarily by means of agricultural production. Business activities that are not agricultural production but involve a firms production, such as marketing livestock or merchandizing grain, are allowed in the firm but not in the farm. Some production activities of the farm that do not lead to the creation of monetary utility are allowed in the farm but not the farm-firm. This may include keeping a registered hog for show purposes. It is possible to further clarify the distinction between 'farm,' 'firm,' and 'farm-firm' by the use of Boolean algebra. Consider the venn diagram shown in Figure 1.


Figure 1. Farm, firm, and exogenous space

Space A, called 'Exogenous', is the compliment or disjoint of spaces B and C. Space B, labelled 'Farm,' includes all the resources, activities, and services related to the physical aspects of agricultural production. Space C, named 'Firm' includes all of the resources, activities, and services related to the business enterprise. The subspace 'B intercept C' is the collection of activities, resources, and services that are referred to as the 'farm-firm' in this study. By mathematical definition it includes only those elements that are members of both spaces $B$ and $C$, i.e. $B \cap C$, such as land owned by the firm and used for raising crops. The subspace that we shall call 'farm-nonfirm' is defined as those elements in space $B$ that are disjoint from space $C$, i.e. $B \bar{C}$ (read ' $B$ not $C$ '). Examples include non-business production activities such as prize hogs, and nonbusiness decisions of the farm family such as taking vacations. The term 'firm-nonfarm' refers to those elements in space $C$ that are not in space $B$, i.e. $C \bar{B}$ (read 'C not $B$ '). This subset includes business activities not directly related to agricultural production such as investment in corporate stock or renting a farm house.

The independence of farm and firm in this study is not clear. For example, it may be necessary for a farmer to borrow short term production capital to finance livestock say, in order to make long term corporate share investments. Under this situation there clearly exists an interrelationship between 'farm' and 'firm' which is broader than our definition of 'farm-firm'. However, since information on 'firm-nonfarm' investment opportunities open to the farm manager are non existent, no attempt to incorporate this was made. Hutchinson (27) recognized (at least implicitly)
the problem of the interrelationship of 'farm' and 'firm' with respect to capital investment and incorporated exogenous investment in his model. This is explained in greater detail later.
2. Investment

Investment is the process of allocating capital in the expectation of receiving a future income stream.

Interest is (a) the return to investment and includes such components as liquidity and time preference, and risk, or (b) the cost of credit. We may divide investments by origin into exogenous or firm investments. Exogenous investments are defined as those where capital is allocated to the firm from an outside source. This investment is commonly called credit and its cost is defined by contractual agreement. In this study short term production credit is not explicitly included for reasons discussed later. Long term financing of land is assumed available on a mortgage basis and is allowed at the current contractual interest rate.

A complication arises with respect to farm-firm investments. Allocations of farm capital to farm production activities have no defined contractual rate of return. A solution to this problem is to impute a rate of interest to farm-firm investments that is based upon the opportunity cost rate of return of an equivalent firm-nonfarm investment. Of the many bases available to estimate this it is important to choose one that might offer a real alternative to the farm-firm investment under evaluation. In this study the rate of return used is five percent on all
investments except land which is six percent. These rates were chosen since the size and term of farm-firm investments is approximately the same as those that might be made in savings and loan associations or mortgage lenders, which currently pay at that rate.

## 3. Returns to entrepreneurship or net profit

We shall use these terms as synonyms in order to cover a broader audience. ${ }^{1}$ We define entrepreneurship as the activity of making available to the firm those resources and services required by it. The return to entrepreneurship, or net profit, is estimated as the gross income generated by the farm-firms activities less rent (return on investment), cost of inputs used in production (operating costs ${ }^{2}$ ), and taxes. Gross income includes all receipts received by the farm-firm and should include inventory changes and capital gains or losses.

While investment functions may pertain to either "natural" or "legal" persons i.e. either actual persons or legal entities such as corporations, entrepreneurship is a function always carried out by a "natural" person.

The entrepreneur of a farm-firm may have zero investment in the business, may contribute no labor to the production process, and thus may only function as a decision maker bringing together those inputs required for the firm to operate. On the other hand the entrepreneur may be the owner

[^1]of all resources and may contribute all of the labor used in production activities of the farm. Both these extremes are atypical of U.S. farm structure. In the farm studied, labor and entrepreneurship, and some investment are supplied by the farm owners.

We have made a distinction between returns to entrepreneurship and the more usual terms of quasi-rent and pure economic profit (Ferguson 13, p. 318) because quasi-rent includes the opportunity cost of the inputs while returns to entrepreneurship does not, and pure economic profit concerns the short run return to fixed inputs whereas returns to entrepreneurship is considered to remain in the long term and is derived from all inputs.

By partitioning returns between labor and management, investment, and entrepreneurship, as defined here, it is possible to compare different farm-firm programs on a consistent basis. The return to entrepreneurship may be considered an efficiency criterion and as a residual may be allocated between consumption, firm-nonfarm investment, and farm-firm investment, as the entrepreneur desires.

## 4. Linear programming

For the moment we shall define linear programming as a computational method used in prescribing production patterns which maximize profits of Eirms, minimize costs of producing a specified commodity, or related types ol aggregative analyses. We shall explain the computational method in greater detail in Chapter IV.
5. Process and activity

In linear programming terminology an activity is an enterprise such as the growing of corn or raising hogs. A process describes the enterprise more specifically. Thus we may have the activity of growing corn by process 1, 2, or 3 , where different processes refer to different fertilizer applications.
6. Shadow price

The shadow price of a resource is its marginal value product. Thus the shadow price of a resource indicates the amount added to profit by a one unit increase in the level of resource available. Only resources which are limiting a plan have positive shadow prices. Shadow prices are of interest since they indicate possible gains in income through acquisition of an additional unit of scarce resource.
C. Summary

In this introductory chapter we have briefly examined the role of farm management and management decisions in successful farm operations. We have seen how complicated the entire management function may be and we have mentioned linear programming as a method of overcoming some of these difficulties. We have, by the explicit defintion of terms, established a common base from which we may now build. Therefore we now continue the analysis by outlining the aims of the study.

## II. OBJECTIVES

The general objective of this study is to apply linear programming methods, as a farm management tool, to the problem of profit maximization on an individual farm-firm. The study attempts to determine the feasibility of providing optimum plans and estimates of the resulting net income for individual farmers when plans are developed directly from their records and are tailored to suit their particular situation and objectives. In addition, the study endeavors to show how the combination of farm activities may alter over time as additional land is acquired.

Within this overall framework specific objectives are:

1. To analyze input-output data from records of a particular farm by programming optimum enterprise combinations and resource supplies of the individual farm-firm.
2. To determine the optimum resource use for the farm-firm by considering only those alternative resource uses consistent with the objectives and plans of the farm manager.
3. To establish the sensitivity of optimum plans. The sensitivity analysis includes:
a) The effect of cost changes on optimum activity levels.
b) The value of changing the resource restraint levels and the interval over which the value is valid. This information is important because it indicates how a problem may be adjusted to increase profit, and when the problem should be recomputed because of cost or price changes.
4. To specify a pattern of grain storage, sales, and purchases consistent with prices, grain use, and storage capacity.
5. To ascertain capital "flows" over a yearly period.
6. To indicate an optimum resource allocation between activities on an expanded land base by examination of several static models.
7. To examine the profitability of a turkey raising enterprise when competing with various other livestock activities for labor and other cropping activities for land.
8. To quantify the optimum farm size for a farm-firm with the activities and resources specified here, operating in the Clarion-Nicollet-Webster soil association area of Iowa.
9. To form a generalized model of the farm-firm so that future information on prices, technology, etc., may be incorporated into the model to give revised and updated farm plans.

Having elucidated the objectives of the study we shall continue by describing the present farm-firm.

## III. THE SETTING OF THE STUDY FARM

As long ago as 1776 Adam Smith noted in his epoch-making book on economic ideology that "the gain in product from the division of labor... is owing to three different circumstances: firstly to the increase in dexterity in every particular workman; secondly, to the saving of time which is commonly lost in passing from one species of work to another; and lastly, to the invention of a great number of machines which facilitate and abridge labor...." (37, p. 13) To the Agricultural Economist nowhere has this phenomenon been more clearly illustrated than in the development of farms over the last decade. The farm analyzed in this study exemplifies this division of labor: a) labor is divided between enterprises so that each man may specialize in a particular area, and $b$ ) modern capital intensive equipment has replaced labor and enhanced its productivity.

The 720 acre farm which is located in Boone County, Iowa, consists of four tracts of land lying along five miles of road (see Figure 2). The farm, whose modus operandi is as a limited liability corporation, is operated by a father and two sons. Each has a particular area of interest within the total farm operation. One is in charge of the intensive and highly mechanized hog system, another tends turkeys, arranges produce sales, and does the bookwork, while the third is primarily involved in crop production. Of the 720 acres, 520 are owned by the corporation, 160 are leased from members of the family and forty acres are leased privately on a 50-50 share basis.
U.S. Highway 30


Figure 2. Location of Highway Farms Incorporated (not to scale).

The farm is located in the Clarion-Nicollet-Webster soil association, an area known for its highly fertile soil. It is completely flat (0 to $4 \%$ slope), well drained, and has a moderate to high level of organic matter.

## A. Present Management Practices

## 1. Hog production

Over 1000 hogs are raised annually. Sows are continuously farrowed in a completely confined central farrowing-nursery house containing 20 farrowing crates and sixteen nursery pens. After weaning at 40 lbs young hogs are transferred to open-shed concrete lots where they are grown out to 220 lbs. The growing lots have a modified cattle auger feed system and automatic heated water troughs.

The insulated farrowing-nursery building has a heated floor, thermostatically controlled ventilation fans which periodically provide an air change, and an automatic watering service. Feed however is carried in by hand.

Manure disposal is effected by sloping floors in the farrowing pens and nursery units leading to a central gutter which in turn carries wastes to a storage pit. The pit is pumped out weekly and the contents spread on the land.

Thus the total farrowing system is designed so that one man can tend the maximum number of litters possible.

Gilts are chosen from litters and are later crossed with boars purchased annually from the Iowa Swine Testing Station. A three way cross
using Durocs, Hampshires, and Yorkshires is currently employed. Sows are kept for about five years before being replaced.

Hogs are sold on the farm to a local buyer.

## 2. Turkey production

Between 12,000 and 13,000 turkeys are raised from day old poults to 28 lb birds, annually. The first of two batches of 6,500 birds arrives in mid March and is sold in mid September, while the second batch is started on 1 June and sold on 1 December.

Poults are brooded in an environmentally controlled insulated building. For the first week of their lives they are kept on peat litter and contained by low corrugated cardboard walls. They are subsequently placed in wire mesh pens with wire floors and kept here for the next five weeks. If weather conditions are suitable, birds are moved outside during the last week of their confinement in order to harden them off and give them the benefit of the sun before being placed on the range. The remaining eighteen weeks of their growing period is spent on the range.

White strains of tom turkeys are raised. Although tests show that bronze strains out-perform whites in feed efficiency, (29) the farm managers raise whites because of the greater net revenue resulting from slightly higher prices received for the more attractive broad breasted white turkeys. Similarly, despite the fact that hens consume less feed per pound of weight gain, toms are chosen because they utilize a higher grain-lower protein ration, giving them a cost advantage over hens.

Although contracts guaranteeing a liveweight price per pound at time of delivery are becoming more common, the farmer sells his flock on the farm to the highest bidder at the time the birds reach market weight.

## 3. Crop production

Because of the high price paid to diverted land under the Federal Government Feed Grain Program, the practice has been to participate in this program up to the legal limit. Thus of the 680 cropable acres corn is only raised on one half of the farm's corn base acreage of 350 acres. That is, 175 acres of corn is grown and a matching 175 acres is placed in meadow and left idle. A further 40 acres are planted in an oat-alfalfa mix and used for pasturing turkeys. The balance of 290 acres is divided between oat and soybean production.

In its first year a crop of oats is harvested from the turkey pasture. A cut of hay is taken from it in the second year, prior to releasing turkeys onto it.

Although the land possesses the potential to produce continuous corn, a haphazard rotation is practiced with the exception of a forty acre rented block which is planted in continuous corn. Land to be cropped is fall plowed for several reasons:

1. The farm enterprises do not include pasturing animals and therefore fallen grain and stalks do not constitute a forage source.
2. Under the present farm organization spring labor is always limiting.
3. Since the soil dries and warms earlier if Fall plowed, Spring tillage and planting may commence earlier.

Six row equipment with a $75 \mathrm{~h} . \mathrm{p}$. tractor is employed and crops are planted in 30 inch rows. Corn is planted at a population density of between 21,000 and 25,000 plants per acre.

Because of the closely spaced rows and high plant populations heavy rates of fertilizer are applied to corn. A typical fertilizer program is: 150 pounds per acre of anhydrous ammonia applied as a preplanting treatment when the land is being tilled in spring; 90 pounds per acre of 6-24-24 N.P.K. applied at planting; and 150 pounds per acre of 0-52-52 plowed down in Fall.

Herbicides (either 2,4-D or atrazine) are applied when corn is four to six inches high, and an insecticide (either aldrin or diazinon) is applied at planting time to control corn borer and other pests. Using the above husbandry the farm yields an average of 125 bushels of corn per acre.

Fertilizer is not applied to soybeans but a herbicide, Amiben, is applied at a rate of ten pounds per acre. Soybeans currently yield forty bushels per acre.

Oats are fertilized when planted with 120 pounds per acre of 30-10-10 N.P.K. giving an average yield of ninety-five bushels per acre.
4. Grain storage

Present facilities allow for storage of 70,000 bushels of grain in a 5,000 bushel corn crib, a 5000 bushel silo, and an assortment of steel bins.

Included in ancillary equipment are two fixed grain driers, a mobile grain drier, and a feed grinding and mixing mill.

In addition to storing Federal Government grain, the corporation stores its own corn, oats, and soybeans. Further, some of the additional corn needed throughout the year for hog production is bought shortly after harvest when its price is lowest and stored in the farm's bins until required.

The corporation's equity on the 520 acres of land and fixed improvements is around sixty percent of its market value. This however does not include 160 acres of freehold land leased by the corporation from family members which will eventually be bequeathed to the younger shareholders of the corporation. Given this situation the firm has no difficulty in arranging either short term working capital loans, or longer term mortgages on property purchases.

It is in this general framework that the study is set. Because of the obvious complexity in designing an optimum farm plan consistent with resource quantities and because of the corporation's desire to expand its total operation in the future, assistance was sought by the operators thus giving this study its origins.

We now have an insight into the current operation of the study farm. The following chapter deals with some theoretical aspects concerned with the method of analysis used in the study.

## IV. TECHNIQUE AND METHODOLOGY OF LINEAR PROGRAMMING

Five basic linear programming models are analyzed in this study, the details of which are described subsequently under the heading "Farm Programming Models."

In this chapter the following items are discussed: Firstly, the origins of linear programming are briefly surveyed; secondly, a general static linear programming model is described; thirdly, the assumptions of the technique are discussed; and finally, three production economics principles important in the understanding of linear programming logic are reviewed.

## A. The Origins of Linear Programming

Historically, the general problem of linear programing was developed and applied in 1947 by George B. Dantzig and Marshall Wood, both mathematicians of the U.S. Department of the Air Force. They proposed that "the interrelationships between the activities of a large organization (should) be viewed as a linear programming type model and the optimizing program determined by the maximization of a linear objective function" (42, p. 17). Equally important was the concurrent development of the simplex algorithm for the solution of a linear program by digital computers, presented by Dantzig to a conference in Chicago, Illinois in 1949 and published in 1951 (9).

Since then linear programming has become an important tool in mathematics, engineering, industrial planning, business and economics.

The history of its use in agricultural economics is almost as old as the method itself. At the same comference at which Dantzig presented his papers, Hildreth and Reiter tendered their contribution, "On the Choice of a Crop Rotation Plan" (24). Since this publication in 1951 the literature of agricultural economics has abounded with applications of the technique to agricultural problems. That this should come to pass is no accident. It is surely because linear programming approximates two essential features of many economic problems. Firstly, in practice economic choices are made between a finite set of competing alternatives, and secondly, the best choice among alternatives is often severely constrained by numerous economic, technological, institutional and social factors.

By 1956, after several problems had been overcome, linear programming was firmly established as a valuable tool in farm management analysis. It was regarded by many as a formalized extension of farm budgeting capable of solving much more complex problems than the latter. One of the noteworthy contributions to this specific area at that time was published by Heady and Gilson (20). They noted the following important conclusion which has served as the rationale for further individual farm management studies. Their research showed "that there is not an optimum set of livestock enterprises or management practices (i.e., level of grain feeding) for all farms, but that recommendations should differ between farms depending on their capital and labor situations, as well as on their ability to stand risks." (20, p. 712) Subsequently, literature dealing with the use of linear programming in farm management has taken two paths. Firstly,
many publications have dealt with the application of original models to various other farm situations, and secondly, others have dealt with modifications of the original model in order to increase its informational content. The reader is referred to Kopetz (34) for details on this latter development.
B. A Mathematical Statement of the General Static Linear Programming Model

At the outset it is necessary to realize that linear programming, like other activity analyses, is entirely mathematical in nature. It was developed primarily as a computational method to deal with the calculation of explicit solutions to complicated practical allocation problems for which numerical data is available. Although programing per se may not be able to tell us anything about a particular part of an economy, it can help us find the implications of the economic information we have assumed. That is, there is a connection between these methods and the much older idea of pricing, implicit or market, of scarce resources. ${ }^{1}$

Generally, programming is concerned with the determination of the optimal solution to a problem. Linear programming involves the maximization or minimization of a linear objective function subject to a set of linear constraints. Thus the general linear programming problem is to find the vector ( $x_{1}, x_{2}, \ldots, x_{n}$ ) which maximizes the linear objective function,

[^2]\[

$$
\begin{equation*}
z=\sum_{j=1}^{n} c_{j} x_{j} \tag{1}
\end{equation*}
$$

\]

subject to the linear constraints

$$
\begin{equation*}
x_{j} \geqslant 0 \quad j=1,2, \ldots, n \tag{2}
\end{equation*}
$$

and

$$
\begin{equation*}
\sum_{j=1}^{n} a_{i j} x_{j} \leqslant,=, \geqslant b_{i} \quad i=1,2, \ldots, m \tag{3}
\end{equation*}
$$

Equation 3 is multipled by -1 where necessary to make all $b_{i} \geqslant 0$. Thus by inclusion of slack variables the equation may be rewritten as

$$
\begin{equation*}
\sum_{j=1}^{n+m} a_{i j} x_{j}=b_{i} \quad i=1,2, \ldots, m \tag{4}
\end{equation*}
$$

where $a_{i j}$ is the input coefficient expressing how many units of resource $i$ are required to produce one unit of activity $j$,
$b_{i}$ is the number of units of the $i^{\text {th }}$ resource available for allocation,
$c_{j}$ is the net revenue per unit of the $j^{\text {th }}$ activity,
$x_{j}$ is the level of the $j^{\text {th }}$ activity,
n is the number of real activities, and
m is the number of disposal (slack) activities.
The mathematical formulation of the programming problem may be stated more compactly in matrix form as:

$$
\begin{align*}
\max & c^{\prime} x  \tag{5}\\
\text { subject to } & A x=b  \tag{6}\\
& x \geqslant 0 \tag{7}
\end{align*}
$$

where
$x$ is the column vector of activity levels,
b is the column vector of resource restrictions,
$c^{\prime}$ is the transposed row vector of net returns, and
A is the mxn matrix of input-output coefficients.
A slight modification of the above model allows the formulation of a parametric programming model. Frequently the researcher wishes to know how the optimal solution of a given linear programming model changes as one of its parameters is altered. As there are three basic sets of data in the model, viz; the $c$ vector, the $b$ vector, and the $A$ matrix, there are three corresponding types of parametric programming operations. Parameterizing the net revenue coefficients, that is, parametric programming of the objective function, the problem may be expressed as:

$$
\begin{array}{r}
\max (c+d)^{\prime} x \\
\text { subject to } A x=b \\
x \geqslant 0 \tag{10}
\end{array}
$$

where $d$ is a vector of identical dimensions as $c$.
Parametric programming is a post-optimal procedure commencing after a solution to the basic linear programming model (where $d=0$ ) has been obtained. Since agricultural product prices typically vary from year to year this modification is very useful in a linear programmed farm management analysis.

For further details on linear programming, its extensions, and its agricultural application, the reader is referred to Dantzig (8) and Heady and Candler (19).

## C. The Assumptions of Linear Programming

Heady and Candler list the four major assumptions made in the application of $l$ inear programming as:

1. Additivity and linearity. The activities must be additive in the sense that when two or more are used, their total product must be the sum of their individual products....
2. Divisability. It is assumed that factors can be used and commodities can be produced in quantities which are fractional units....
3. Finiteness. It is assumed that there is a limit to the number of alternative activities and to the resource restrictions which need be considered....
4. Single value expectations. In general... (the assumption is made) that resource supplies, input-output coefficients, and prices are known with certainty. (19, p. 17)

These assumptions are not as restrictive as superficially appears. It has been adequately demonstrated elsewhere that the linear programming model is a logical extension of linear economic theory which is itself a restatement of the conventional theory of competitive equilibrium (12, ch. 13 and 14). In fact "linear programming is marginal analysis appropriately tailored to a finite number of activities" (12, p. 133).

If the assumption of a homogenous production function of degree one, which is the basis of this theory, is acceptable, it is difficult to argue with the linearity assumption employed in programming. ${ }^{1}$ However because of resource indivisabilities variable proportions may have to be admitted in some cases. Fortunately such a situation may be approximated by means

[^3]of a series of linear segments. ${ }^{1}$
The divisability assumption, while a necessary mathematical requirement in the simplex method, may be adapted to the particular empirical problem. Thus if the solution specifies that 452.37 acres of corn be grown, we may reasonably ignore the decimal figure. Indeed, we may even feel justified in rounding off even further and reporting the answer as 450 acres. For other programming problems where a fractional answer is totally meaningless and unacceptable a modification known as integer programming ${ }^{2}$ may be used. Thus the divisability assumption is not as restrictive as it may first appear.

The additivity assumption may impose certain limitations. It does not permit, for example, a complementary relationship between any two activities.

The finiteness assumption also, while a necessary mathematical requirement, does not impose any restrictions in empirical investigations. It is true that fertilizer, for example, may be applied in infinitesmally small increasing amounts on a farm. A farmer however is far from interested in considering this number of alternatives. We may therefore only include three or four discrete levels in an analysis. Besides the practical side which renders the finiteness assumption non-restrictive, the degree of finiteness depends on the capacity of the computer being used to

[^4]solve the problem. Modern computers now have the capacity to handle several thousand activities and as a consequence the finiteness assumption does not become circumscriptive.

The assumption of single valued expectations while certainly unrealistic for some farming situations may be partially overcome by the use of parametric techniques previously mentioned where resource supplies, prices, and input coefficients, are allowed to vary. This modification however does not explicitly consider the effects of, for example, weather variability or risk aversion. Thus a better solution to the problem of variability or risk in programming analyses is to use stochastic linear programming, where we assume that some coefficients are random variables. Examples and explanation of the use of this technique may be found in Beale (2) and Candler (5).

We have now found that in empirical analyses the assumptions of linear programming are not so restrictive as to limit the usefulness of the technique.

## D. Principles Involved in Combining Farm Enterprises

Three basic production economics principles are involved in this study: the factor-product relationship; the factor-factor relationship; and the product-product relationship. Since an understanding of these principles enhances our recognition of problems involved in integrating many farm activities into an overall profit maximizing plan, a modified version of them, depicting linear relationships as assumed in this study,
will be presented.

1. The factor-product principle

This principle concerns changes in output of a given product resulting from changes in the level of inputs used in its production. The classical production function,

$$
\begin{equation*}
\mathrm{y}=\mathrm{f}\left(\mathrm{x}_{1}, \mathrm{x}_{2}, \ldots, \mathrm{x}_{\mathrm{n}}\right) \tag{11}
\end{equation*}
$$

is assumed to be a single-valued continuous function with continuous first- and second-order partial derivatives at every point on the function, where

$$
\begin{aligned}
\mathrm{Y}= & \text { the quantity of output of a given product } \\
\mathrm{x}_{1}, \mathrm{x}_{2}, \ldots, \mathrm{x}_{\mathrm{n}}= & \text { the quantities of inputs used in the production } \\
& \text { of } \mathrm{Y} \text {, and } \\
\mathrm{f}= & \text { some mathematical function. }
\end{aligned}
$$

If we now vary $x_{1}$ holding all other factors fixed then we may derive a production function similar to that shown in Figure 3. It will be continuous and the point of profit maximization will be that unique point where the slope of the production function equals the inverse price ratio of the product and factor. That is, the equilibrium position is where

$$
\begin{equation*}
\frac{\mathrm{dy}}{\mathrm{dx}}=\frac{\mathrm{P}_{\mathrm{x}}}{\mathrm{P}_{\mathrm{y}}} \tag{12}
\end{equation*}
$$

where $P_{x}=$ the unit cost of $x_{1}$
and $\quad P y=$ the unit price of $Y$.
In the case of linear programming analyses, the production function is discontinuous being represented by a series of linear segments as shown in Figure 3. At a point of discontinuity there does not exist a uniquely


Figure 3. A discontinuous production function; the response of product $Y$ to discrete changes of factor $X_{1}$
defined plane tangential to the isoquant thus the equilibrium equation above cannot be used. Instead, the equilibrium position is found where the following inequalities hold:

$$
\begin{equation*}
\frac{d y^{\ell}}{d x_{1}^{\ell}} \geqslant \frac{P_{x}}{P_{y}} \geqslant \frac{d Y^{r}}{d X_{1}^{r}} \tag{13}
\end{equation*}
$$

where $\frac{d Y^{\ell}}{d X_{1}^{\ell}}=$ the left-hand partial derivative at the given point, and $\frac{\mathrm{dy}}{\mathrm{dx}} \mathrm{X}_{1}^{\mathrm{r}}=$ the right-hand partial derivative at the given point. At
the given point. At any point where there is no discontinuity the righthand and left-hand derivatives are identical hence the inequality converges to the equality

$$
\frac{\mathrm{dy}}{\mathrm{dx}} \mathrm{x}_{1}=\frac{\mathrm{Px}}{\mathrm{Py}}
$$

which is the same as equation 12 for the continuous case. In the discontinuous case however, when equation 12 occurs, the equilibrium is not a unique one.

## 2. The factor-factor principle

This principle is concerned with the substitution of one resource for another in the production of a given quantity of product. In the two factor case the expression for this relationship is,

$$
\begin{equation*}
\mathrm{Y}=\mathrm{f}\left(\mathrm{X}_{1}, \mathrm{x}_{2}\right) \tag{14}
\end{equation*}
$$

where $X_{1}$ and $X_{2}=$ two substitutable resources used in the production of $Y$, a fixed level of output. The locus of all the combinations of $X_{1}$ and $X_{2}$
which satisfies equation 14 forms an isoquant. When the production function is continuous so too is the isoquant, its slope at any point giving the marginal rate of substitution of $X_{1}$ for $X_{2}$. If we let the factors $X_{1}$ and $X_{2}$ represent quantities of corn and oats used in the production of 100 pounds of pork ( Y ) then the least cost combination of producing 100 pounds of pork from corn and oats is found by equating the marginal rate of substitution with the inverse price ratio. That is,

$$
\begin{equation*}
-\frac{d x_{2}}{d x_{1}}=\frac{P x_{1}}{P x_{2}} \tag{15}
\end{equation*}
$$

Given that the isoquant is 'well-behaved' this relationship gives a unique solution. In linear programming however the isoquant is formed from several discrete processes and as such consists of a series of linear segments as depicted in Figure 4. The least-cost combination of the two resources is where an isocost line just touches or is "tangential" to the isoquant. If "tangency" occurs on a corner as shown in Figure 4 then the least cost combination is stable over the range of resource prices

$$
\begin{equation*}
-\frac{d x_{1}^{\ell}}{d x_{2}^{\ell}} \geqslant \frac{P x_{2}}{P x_{1}} \geqslant-\frac{d X_{1}^{r}}{d x_{2}^{r}} \tag{16}
\end{equation*}
$$

This is one reason why a linear program can give the same solution over a range of prices. On the other hand if the price ratio (isocost line) has the same slope as one segment of the isoquant then there are many different resource combinations which give the same product at the same minimum resource cost.


Figure 4. Different processes for the activity of producing 100 pounds of pork from corn and oats
3. The product-product principle

This principle is concerned with the optimum combination of products given a fixed quantity of resources. In its implicit form it may be expressed as

$$
\begin{equation*}
\mathrm{f}\left(\mathrm{Y}_{1}, \mathrm{Y}_{2}, \mathrm{X}\right)=0 \tag{17}
\end{equation*}
$$

Assuming that equation 17 can be solved explicitly for $X$, then

$$
\begin{equation*}
\mathrm{X}=\mathrm{f}\left(\mathrm{Y}_{1}, \mathrm{Y}_{2}\right) \tag{18}
\end{equation*}
$$

In this example let $Y_{1}$ be bushels of corn produced, $Y_{2}$ be bushels of oats produced, and X be the quantity of labor available. In addition we shall assume there is a maximum quantity of corn that can be produced on the given land. A production possibility curve (product transformation curve) is defined as the locus of output combinations that can be secured from a given input quantity $x$.

In its continuous form a"well-behaved" production possibility curve is concave to the origin due to the changing marginal rate of transformation of resource into products. In a linear programming analysis we assume that the marginal rate of transformation is constant however restraints, such as a maximum corn acreage or total available labor in our example, restrict the feasible area so that the production possibility curve, although consisting of segments, is likewise concave to the origin. This is presented in Figure 5. As with the previous principles the conditions of constrained revenue maximization used in the case of continuous functions cannot be employed. Instead we specify that for constrained


Figure 5. A linear programming representation of a product transformation function and isorevenue line, showing the point of constrained maximum profit, A
revenue maximization it is necessary that the inequality

$$
\begin{equation*}
-\frac{d Y_{1}^{\ell}}{d Y_{2}^{\ell}} \geqslant \frac{\mathrm{Py}_{2}}{\mathrm{Py}_{1}} \geqslant \quad-\frac{\mathrm{dY}}{1} \mathrm{dY} \tag{19}
\end{equation*}
$$

hold. As explained with previous principles this equilibrium will be stable over a range of prices.

A detailed account of the preceding principles may be found in Heady (18) chapters 2 through 8 and Henderson and Quant (23) chapter 3. For a discussion on the relationship between continuous and discontinuous functions the reader is referred to Samuelson (35, p. 70).
4. Integration of the factor-factor and product-product principles

If the factor-factor isoquant of Figure 4 were superimposed upon the product transformation function of Figure 5, then, ignoring price relationships, the optimum point of integration between the two crops and the hog ration occurs where the two functions just touch, i.e. at point A in Figure 6.

Whilst many farmers may think in terms of Figure 6, producing feeds in the same proportion as they feed it to their livestock, it is possible for them to improve their profit position by considering the relative prices of the crops. Since both corn and oat grains are negotiable it is possible for farmers to sell one grain and purchase the other if relative prices so dictate. Referring to Figure 7 if both grain crops and hogs were produced according to relative prices grains would be produced in amounts represented by point $B$ and hogs would be fed grains in proportions

Figure 6. Integration of the grain transformation function with the pork isoquant

represented by point $A$. This being the situation $O C$ of oats and $O D$ of corn will be produced while OE of oats and OF of corn will be fed to hogs. Accordingly, CE of oats will be sold and DF of corn will be purchases. The principle illustrated in Figure 7 was permitted to operate in the linear programming models about to be described. Several buying and selling activities for different types of livestock at different times of the year and for the various crops were included in the model to give the farm-firm maximum flexibility and to allow profit maximization within the resources available.

In this chapter we have outlined the history of linear programming, described the general linear programming model and a modification of it, and discussed the assumptions implicit in a linear programming analysis. In addition we have taken a cursory examination of three basic production economics principles and we have seen how they relate to linear programming. In the succeeding chapter we shall describe the models constructed to depict various farm situations.

## v. FARM PROGRAMMING SITUATIONS

In building a linear programming model Dantzig (8) recommends the following steps be taken:

Step 1: Define the Activity Set. Decompose the entire system under study into all of its elementary functions, the activities, and choose a unit for each activity in terms of which its quantity, or 'level', can be measured.

Step 2: Define the Item Set. Determine the classes of objects, the 'items', which are consumed or produced by the activities, and choose a unit for measuring each item. Select one item such that the net quantity of it produced by the system as a whole measures the 'cost' of the entire system.

Step 3: Determine the Input-Output Coefficients....
Step 4: Determine the Exogenous Flows. Determine the net outputs or inputs of the items between the system, taken as a whole, and the outside.

Step 5: Determine the Material Balance Equations....for each item write down the material balance equation which asserts that the algebraic sum of the flows of that item into each activity is equal to the exogenous flow of the item.

The result of model building thus, is the collection of mathematical relationships characterizing all feasible (or acceptable) programs of the system. This collection is the linear programming model, and the above steps will be followed in constructing the models used in this study. In every case, all enterprises and restraints which might enter into the farm situation were developed in close consultation with the farm operators.
A. Model 1

This model is designed to indicate the optimum allocation of resources between presently practiced enterprises and the level of these enterprises
on the study farm. The optimum allocation of resources is defined as that allocation which maximizes profit. Only activities presently employed and resources and facilities presently available are considered. Any difference between the optimized solution of this model and present farm situation should indicate adjustments possible within the present farm structure capable of improving net profit.

Step 1. Activities or enterprises:
a. Crop enterprises: Typically, central Iowa farmers produce four crops, viz., corn, oats, soybeans and meadow. Although the usual husbandry involves a rotation of some combination of these, the study farm does not practice a set rotation because soil conditions and pest problems are such that conuous monocropping may be practiced if desired. Despite carryover effects which invariably exist between a crop planted in one year and a crop planted on the same area in the preceeding year, these interrelationships are assumed away in the model since fertilizer applications are always heavy and crop yields consistently high regardless of the previous land use.

One level of fertilization for those crops fertilized is considered, this level being the usual application used on the farm as detailed on page 18 .

Since payment received from the Federal Government for diverted land under the Feed Grain Program decreases as the proportion of a farm's corn base acreage placed into diverted acres increases, it was necessary to incorporate a "multiple right-hand side" routine into the program (3, p. 77).

This allows a comparison of the profitability of different degrees of participation to be made with non-participation.

Figure 8 shows how this portion of the model was constructed. It is necessary to construct the model in this form in order that it behave in a manner portraying reality. The usual way of incorporating activities using land would be to have each activity use an acre of the total land resource and limited to some maximum acreage. Since $20 \%$ diverted land receives a higher payment than $40 \%$ diverted land which in turn receives a larger payment than $50 \%$ participation in the grain program as shown in Table 1, it is not reasonable to set the model up in that form. If it were and if diverted land were to enter at the $50 \%$ level then the program would bring the highest returning $20 \%$ diverted land in up to its limit, and then bring the $40 \%$ diverted land in up to its limit, and fill the remaining $10 \%$ with the lowest returning $50 \%$ diverted land. This possibility must be excluded from the program as farmers do not get paid for diverted land in that manner. Accordingly the model was built as shown in Figure 8 and operated as is now described.

In the first computer "run" only 'Land C' and 'RHSA' of the resources shown are at non zero levels. This configuration excludes diverted land from entering the solution allowing the program to select that combination and area of the specified crops (corn, oats, soybeans, and turkey pasture) that is consistent with the resource restraints yet maximizes profit. By altering the resource quantity of RHSA the program may be restricted to prodicing a maximum acreage of corn as specified by that quantity.

The second right hand side "run" involves setting Land B at 350 acres,

| Resource |  | Diverted land |  |  | Corn 1and supply |  |  | Oats | Soybeans | Turkey pasture |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Quantity | 20\% | 40\% | 50\% | 1 | 2 | Corn |  |  |  |
| Land A | 0 |  |  |  | -1 | -1 | 1 |  |  |  |
| Land $B$ | 0,350 | 1 | 1 | 1 | 1 |  |  |  |  |  |
| Land C | 680 | 1 | 1 | 1 | 1 | 1 |  | 1 | 1 | 1 |
| RHS A | 0,680 |  |  |  |  | 1 |  |  |  |  |
| RHS B | 0, 70 | 1 |  |  |  |  |  |  |  |  |
| RHS C | 0,140 |  | 1 |  |  |  |  |  |  |  |
| RHS D | 0,175 |  |  | 1 |  |  |  |  |  |  |

Figure 8. A portion of the initial L.P. tableau showing incorporation of diverted land

Table 1. Crop prices used in the study

${ }^{\text {a Capital }}$ letters refer to respective months.

Land C at 680 acres, RHSA at zero and RHSB at 70 acres. By doing this diverted land may now enter up to a limit of $20 \%$ of the total corn base acreage ( 350 acres). Further, the total area of corn is limited to the balance of 350 acres after diverted acres (if they enter the plan) have been subtracted. This is effected by the use of "corn land supply" columns as shown. If the program has selected corn and/or diverted land, the area they occupy is deducted from the total farm acreage and the balance may be allocated to any of the other crops as selected by the computer.

The third right hand side requires that RHSB be set to zero and RHSC be set to 140 acres. Similarly the fourth right hand side has RHSB and RHSC set at zero while RHSD enters at 175 acres. The mechanizm for these is the same as that described for the second right hand side except that diverted land may enter up to a maximum of $40 \%$ of the corn base acreage in the case of the third right hand side and up to $50 \%$ in the case of the fourth right hand side.

Corn grain produced may be fed to livestock or sold. Since corn silage is not a useful intermediate product in hog and turkey production it is not included in this model.

Corn may also be purchased or sold in any of four quarterly periods defined in Table 1, at the indicated prices. Likewise if oats and/or soybeans are produced they may be sold in any of the four periods at specified prices. Grain prices used in the study are based on the latest four year monthly averages (28).

Since grain storage is limited to 70,000 bushels, multiple grain merchandizing activities together with dated livestock grain consumption allow the program to simultaneously solve the grain inventory problem. The problems in building a model that does this together with an explanation of the model are given subsequently (pages 56 to 60 ).

Straw produced from oat production is utilized on the farm as bedding for livestock.
b. Livestock activities: Thirteen livestock activities are included in model 1. With the exception of a turkey producing activity, all concern hog production. Since model 1 is intended to indicate possible reorganization of activities presently employed, cattle are excluded from the analysis. In subsequent models they may enter. Hogs may be raised from weanlings produced on the farm or from purchased weanlings. Also weanlings produced on the farm may be sold at 40 pounds. Each of these activities are divided into four three-monthly periods. The reason for doing this is to reflect seasonal price differences (as denoted in Table 2) and to allow the program to select the optimum integration of these activities, in terms of their resource requirements, with other activities. Thus we may find that during winter months when no labor is required for crop production, some of the hog activities enter the program at the maximum level, whereas in spring when labor may become limiting, hog production is reduced in order to allow the labor to be used for crop planting.

Other activities in the model are included for functional purposes only.

Table 2. Livestock prices used in the study (selling prices $\$ /$ head)

| Livestock activity | Selling period | Gross price | Net price |
| :---: | :---: | :---: | :---: |
| Hogs 1 | DJF | \$ 39.32 | \$26.65 |
| Hogs 2 | MAM | 35.97 | 23.22 |
| Hogs 3 | JJA | 42.43 | 29.68 |
| Hogs 4 | SON | 37.74 | 25.07 |
| Feeder hogs 1 | DJF | 38.50 | 15.28 |
| Feeder hogs 2 | MAM | 35.22 | 12.42 |
| Feeder hogs 3 | JJ A | 41.58 | 16.58 |
| Feeder hogs 4 | SON | 36.96 | 14.95 |
| Weanlings 1 | DJF | 16.92 | 8.68 |
| Weanlings 2 | MAM | 16.55 | 8.45 |
| Weanlings 3 | JJA | 17.65 | 9.60 |
| Weanlings 4 | SON | 15.98 | 7.78 |
| Turkeys (10 birds) | $S$ and D | 56.00 | 33.13 |
| Steer calves 1 | Aug | 278.50 | 111.95 |
| Steer calves 2 | Aug | 278.50 | 119.78 |
| Yearlings 3 | April | 274.60 | 88.26 |
| Yearlings 4 | April | 274.60 | 90.53 |
| Steers 3 | Sept. | 271.80 | 74.09 |
| Steers 4 | Sept. | 271.80 | 75.33 |
| Both yearlings and steers 3 | AP and $S$ | 546.40 | 171.36 |
| Both yearlings and steers 4 | Ap and S | 546.40 | 175.33 |

Step 2: The Item Set (resource restraints):
a. Land: Since model 1 depicts the study farm in its present form, the area of land involved is 720 acres. Forty acres of this are covered by buildings, yards, roads, etc., leaving 680 acres of cropping land. Since fertilizer treatments and crop response are the same over the total area, the division of land into soil types was not necessary.
b. Labor: Presentiy the farm is operated by three labor units giving a total of 36 months of man labor per year. The labor supply is divided into five periods in order to reflect differing seasonal labor requirements. The maximum number of hours per period which the labor is prepared to work was determined by communication with the farm-firm operators. By examination of the quantity of labor in each period indicated in the optimal solution of the program, it is possible to specify the periodic labor requirements necessary if the plan is to be implemented. It is assumed that all activities requiring labor draw it from the total i.e. no custom work is allowed. It is possible however to hire an additional labor unit on a permanent basis. The operators feel that the firm would hire additional labor if it were profitable but because part time labor is difficult to obtain at crucial periods the only alternative the firm would consider is hiring a permanent full-time hand. The maximum available labor hours per period for three, four and five labor units is presented in Table 3. Hiring an extra labor unit adds $\$ 8,000$ to the fixed cost of the firm.
c. Livestock restrictions: A maximum of 500 piglets may be farrowed and nursed over any three month period in facilities described previously.

Table 3. Distribution of the firm's labor supplya

|  | Working <br> days | Maximum hours per |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | labor <br> unit | 3 units | 4 units | 5 units |  |  |
| Dec.Jan.Feb. |  | 6 | 432 | 1296 | 1728 | 2160 |  |
| March April |  | 8 | 384 | 1152 | 1536 | 1920 |  |
| May June |  | 11.5 | 552 | 1656 | 2208 | 2760 |  |
| July Aug |  | 8.5 | 408 | 1224 | 1632 | 2040 |  |
| Sept.Oct.Nov. | 72 | 10 | 720 | 2160 | 2880 | 3600 |  |
| Total | 288 |  | 2496 | 7488 | 9984 | 12480 |  |

${ }^{a}$ Source: Private communication with firm managers.

Space for growing-finishing hogs is limited to 420 hogs per period.
The maximum number of turkeys that may be raised annually, due to building limitations, is 20,000 birds.
d. Capital: Only operating capital is considered in the study in the manner shown in Figure 9. Capital expenditures and receipts are dated and placed into the relevant capital supply row. The numerals on the rows indicate the quarter of the year and correspond to those on livestock and grain activities. Four capital transfer columns allow surplus or deficit capital in any one period to be carried over to the next. Capital remaining in the fourth period is transferred back to the first period. It will be noted that the level of 'capital supply $l$ ' is zero rather

than being at some positive level (indicating the quantity of working capital available at the beginning of the production year) as is frequently found in similar linear programming models. The reason for constructing our model in this way is to allow the program to dictate what quantity of capital should be available at the beginning of that period. Thus in the optimal solution the entry found on 'capital transfer column $4^{\prime}$ indicates that sum of cash that should be on hand at the beginning of the first period (end of the fourth period) if the optimal plan is to be implemented. Although borrowing is not explicitly included in our model it is easy for the farmer to find out how much he must borrow. Since the program tells us what quantity of capital must be available at the beginning of the production year if the plan is to be executed, then the difference between that sum and what the farmer actually has on hand represents the total that he must borrow or will have as a surplus.

Fixed costs (which include salaries) are endogenously deducted from the capital supply by means of fixed cost paying activities. Annual fixed costs are divided equally between the four quarters and paid accordingly. ${ }^{1}$

Since no entry was made in the objective row for the fixed cost paying activities the objective function gives the gross returns resulting from the optimal plan whereas the capital supply rows indicate the net returns that would result.

[^5]Capital transfer columns indicate the quantity of capital carried over from one period to the next. Thus it is possible to observe the quantity of capital available at the end of any period and to trace the annual pattern of capital "flows" over discrete three month intervals if the plan is followed.

Capital borrowing is not explicitly allowed because as the model depicts an equilibrium situation the program would not borrow in any period unless it could repay it in another, and since the objective function is always positive in this model, this is always the case. If borrowing were incorporated into the model the program would need to repay capital borrowed in one period in the next period and this activity would compete with the capital transfer rows. If, on the other hand, a large enough sum of capital is on hand at the beginning of the year the program will not need to borrow. Hutchinson (27) incorporated borrowing into his study by allowing the program to borrow and repay over a three month period, and also allowing it the opportunity to invest capital exogenously for a minimum of six months. While this approach has some merit it was not considered in our study because of the numerous exogenous investments available and their often unknown return.

Step 3. Input-output coefficients:
Input-output coefficients were derived from a wide variety of sources, primary ones for the various categories of data being given below.

Present farm situation: Background information on cropping patterns, crop yields, fertilizer and therapeutant treatments, hog and turkey produc-
tion systems, and general farm operations, were obtained from interviews with the farm manager. Specific details on feed consumption and costs, labor charges, taxation, interest payments on mortgages, depreciation, etc., were supplied from the firm's records.

Labor coefficients: Since records of labor utilization were not kept on the study farm, it was necessary to obtain these from other sources then modify them in consultation with the farm operators. Labor coefficients were obtained from the following sources: a) cropping labor coefficients were obtained from James (30), b) swine labor coefficients were modified from Trede (39), c) Turkey labor coefficients were derived from a study of Iowa turkey producers (29), and d) cattle labor coefficients were obtained from Hutchinson (27). Actual labor coefficients used in the study may be found in Table 24.

Costs: As is of ten the convention, input costs are divided into two general categories. a) fixed costs; those that are incurred irrespective of the level of production, e.g. depreciation and property taxes, and b) variable costs; those that vary with the level of production, e.g. fuel and fertilizer costs.
a. Fixed costs: Data on capital expenditures of buildings, machinery, and equipment, were obtained where possible from the farm depreciation schedule. Otherwise, the replacement cost of each item was calculated by deducting the trade-in value of the replaced item from the new cost of the replacement item. Straight line depreciation as used in the farm
records was used to calculate annual depreciation. Machinery and equipment repair costs are charged at three percent per annum of the replacement cost and building repairs at one and one half percent of the new cost. Taxes and insurance are calculated at two percent per annum of the replacement cost of machinery and equipment, and at 1.3 percent of the new cost of buildings (after D. A. Hull et al., 26). Interest on capital invested in machinery, buildings, and equipment, is calculated at five percent ${ }^{1}$ of the average value of the item, where the average value is fifty percent of the replacement cost (after E. O. Heady, et al., 22).

In the case of hog and turkey facilities, the cost of constructing a similar building and equipment was found and annual fixed costs derived accordingly. The reason for doing this rather than using the actual farm values and depreciation was because many buildings have been considerably modified in terms of their associated equipment. This equipment has of ten been installed by the operators thus the labor costs associated with it, and the actual equipment costs do not appear in the structures total cost. Further, some buildings are used for turkey production over spring and summer, and for hog production over winter. To overcome these complications, the cost of replacement buildings and equipment were used. The itemized capital cost of these structures may be found in Tables 12, 13, and 14.

[^6]A schedule of machinery on the farm, and its annual fixed costs may be found in Table 9, whilst a similar schedule of fixed costs of buildings and equipment may be found in Table 11. Table 17 summarizes all the fixed costs considered in the study.
b. Variable costs: Tractor operating costs are itemized on Table 4 while Table 6 details the total variable costs associated with crop production. Tables 7 to 10 itemize the variable costs and revenue of the livestock activities.

## B. Model 2

In construction this model is almost identical to model 1 differences being that cattle activities, larger resource quantities, and altered input-output coefficients, have been added. In this model eight row cropping equipment has replaced six row equipment used in model 1 with consequent changes in labor coefficients and cost entries. Sixteen cattle feeding activities have been added. These are:
(a) Feeding steer calves: Calves may be purchased in November at 450 lbs and raised in feedlots until they reach a weight of 1050 lbs in August. Calves may be fed on either of two rations, and may be fed by a self-unloading wagon method, or a conveyor feeding system. In the model these four activities are called "Calf---", where the first digit indicates the ration, the letter " A " denotes a self unloading wagon feeding system, and " $B$ " indicates a conveyor feeding system.
(b) Fall feeding yearling steers: Steers may be purchased at 600 lbs in October and sold at 1050 lbs in April. They may be fed either of two rations, and may be fed by either of the two systems outlined above. These activities are termed "Yrlg.---" in the program where the nomenclature is the same as previously explained.
(c) Spring feeding yearling steers: In late April 700 lb steers may be purchased for sale at 1050 lbs in September. As with (a) and (b) they may be fed either of two rations by either of two feeding systems. These activities are named "Steer---".
(d) Feeding Spring steers and Fall steers: These activities are merely a combination of (b) and (c) activities. Since Fall fed steers occupy the feedlot for 190 days from October until early April, and Spring fed steers require the same facilities for 145 days from late April to September, it is possible to combine these activities into one. As with other cattle activities they may be fed either ration by either feeding method. In the program these activities are denoted as "Both---".

Further details of input-output coefficients, costs, and returns, are given in Tables 15 and 16 .

Since there are presently no cattle feeding facilities on the farm all costs associated with raising beef are allocated between each animal. This procedure assumes constant costs and perfect divisability of facilities over the entire range, a somewhat heroic assumption at the extremes, i.e. for enterprises raising fewer than 300 head or more than 1200 head, but probably a reasonable approximation within those limits. Each cattle
beast raised requires . 004 acre of land, or approximately 180 square feet. The cattle land requirement is subtracted endogenously in the model.

Hogs, feeder-pigs, and weanlings may be raised in facilities described previously. In addition, once the facilities reach maximum capacity, the relevant expansion activity of the twelve different swine activities may enter the model. Expansion activities are identical to their corresponding regular activity except that capital costs associated with the production of swine which were considered fixed in the regular activities are allocated as a per hog per year cost in the expansion activities. As with the cattle activities constant scale returns are assumed.

In a similar manner turkey production may exceed the capacity of present facilities by a turkey expansion activity. This activity also has all capital costs associated with turkey production allocated as an annual per bird cost.

The possibility of hiring one or two extra labor units is allowed in model 2. A maximum of two hired hands was selected arbitrarily by the operators as the maximum number of men they would want to supervise.

A further modification made in this model is the addition of an activity which allows grain bins to be purchased. If it is profitable to employ additional grain storage the model will do so thus indicating the optimum storage capacity that the farm-firm should utilize.

At this point it is appropriate to explain the operation of the grain inventory portion of the linear programming model as depicted in Figure 10.

Since grains may be purchased and sold at varying prices at different times of the year, since grain consumption by farm livestock occurs unevenly over the year whilst production eventuates at a specific time, and since grain storage capacity is limited or can only be expanded at some cost, there clearly exists a grain storage inventory problem, the solution to which is that pattern of corn purchases, grain sales, and storage bin investments that will maximize profits.

In terms of total storage capacity the following equality must hold.

$$
\begin{equation*}
S_{t-1}+P_{t}+B_{t}=U_{t}+Q_{t}+S_{t} \tag{20}
\end{equation*}
$$

where
$t=t$ he time period,
$S=$ the quantity of grain in storage,
$P=$ grain produced,
$B=$ grain bought,
$\mathrm{U}=$ the quantity of grain utilized as animal feed, and
$Q=$ the quantity of grain sold.
In Figure 10 , which is based on equation 20 , time periods representing quarterly terms coincidental with quarters used in grain and hog activities, provide rows into which coefficients from activities requiring grain storage are placed. It was recognized that once grains enter storage they lose their identity. Consequently, unless structured otherwise, when livestock require a quantity of corn from storage, the program, failing to distinguish between corn, oats, and soybeans, will feed livestock with the lowest priced grain, namely oats. So that this complication

| Resource |  | Corn | Oats | Beans | Buy | corn |  | Se |  | cor |  | $\begin{gathered} \text { Corn } \\ 1 \end{gathered}$ | $\begin{aligned} & \text { stor.trans. } \\ & 2 \end{aligned}$ |  |  | Corn transfer |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | (acre) | (acre) | (acre) | 12 |  | 4 | 1 | 2 | 3 | 4 |  |  |  |  |  | 3 |  |
| Corn production | $0 \geqslant$ | -125 |  |  |  |  |  | 1 | 1 | 1 | 1 |  |  |  |  |  |  |  |
| Oatgrain | $0 \geqslant$ |  | -95 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Soybeans | $0 \geqslant$ |  |  | -40 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Time period 1 | $0=$ |  |  |  | -1 |  |  |  |  |  |  |  |  |  |  |  |  | 1 |
| Time period 2 | $0=$ |  |  |  | -1 |  |  |  |  |  |  |  |  |  |  |  | -1 |  |
| Time period 3 | $0=$ |  |  |  |  | -1 |  |  |  |  |  |  |  |  |  | -1 |  |  |
| Time period 4 | $0=$ |  |  |  |  |  | -1 |  |  |  |  |  |  |  |  | -1 |  |  |
| Time period 11 | $0=$ |  |  |  |  |  |  | 1 |  |  |  | 1 |  |  | -1 |  |  | 1 |
| Time period 22 | $0=$ |  |  |  |  |  |  |  | 1 |  |  |  | 1 |  |  |  | 1 |  |
| Time period 33 | $0=$ |  |  |  |  |  |  |  |  | 1 |  |  | -1 | 1 |  |  | 1 |  |
| Time period 44 | $0=$ | -125 |  |  |  |  |  |  |  |  | 1 |  |  | -1 | 1 | 1 |  |  |
| Time period 1A | $0=$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Time period 2A | $0=$ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Time period 3A | $0=$ |  | -95 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Time period 4A | $0=$ |  |  | -40 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Gr.store max. 1 | 70000 |  |  |  |  |  |  |  |  |  |  | 1 |  |  |  |  |  |  |
| Gr.store max. 2 | 70000 |  |  |  |  |  |  |  |  |  |  |  | 1 |  |  |  |  |  |
| Gr.store max. 3 | 70000 |  |  |  |  |  |  |  |  |  |  |  |  | 1 |  |  |  |  |
| Gr.store max. 4 | 70000 |  |  |  |  |  |  |  |  |  |  |  |  |  | 1 |  |  |  |

Corn consump| 0 |
| :--- |
|  |




$$
\begin{aligned}
& 0 \\
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& 0 \\
& 0 \\
& 0 \\
& \omega \\
& \infty
\end{aligned}
$$


Corn production 0
Corn production
Oatgrain
Soybeans
Time period 1
Time period 2
Time period 3
Time period 4
Time period 11
Time period 11
Time period 22
Time period 33
Time period 1A
Time period 2A
Time period 3A
Time period 4A
Gr.store max. $170000 \geqslant$
Gr. store max. $270000 \geqslant 1$
Gr.store max. $370000 \geqslant$
a Bought corn transfer.
$b_{\text {Buy grain storage. }}$
could not arise corn was placed into separate time period rows from soybeans and oats. Thus producing an acre of oats requires 95 bushels of storage capacity in the third period ('time period 3A'), buying a bushel of corn in the second period utilizes one bushel of storage space in 'time period 2', and raising hogs for sale in period one adds to the storage space in all four periods as corn is consumed. Four 'grain storage' activities transfer oats and beans remaining at the end of one period into the next period. They also transfer the balance into corresponding 'grain storage maximum' rows, which enforce the restriction that total grain stored per period may not exceed 70,000 bushels. Four activities named 'bought corn transfer' allow the balance of bought corn and corn consumed by livestock to be transferred from one period to another. Additionally they transfer the balance into 'grain storage maximum' rows in an identical way as was done for oats and soybeans. The reason that it is necessary to include 'time period' rows, which are set equal to zero, is so that the act of transferring grain from one period to the next will not add to the grain storage capacity as would otherwise occur. A 'buy grain storage' activity allows storage bins to be purchased at 5.6 cents per bushel and adds one bushel of storage to each 'grain store maximum' row.

Initially this was how the grain inventory problem was built. However a difficulty was encountered. It proved profitable for the program to buy grain storage ad infinitum filling it with corn purchased in period four and storing it for sale in period three. That is, the farm-firm was
to become a grain dealer. This problem was rectified by separating produced corn from bought corn. It was therefore necessary to add four more time period rows, 'time period $1: 1$ to $4: 4^{\prime}$. Corn raised on the farm goes into 'time period $4: 4^{\prime}$ since corn is harvested in the fourth period. From here it may be transferred to any other period by four 'corn storage transfer' activities. As with previously described grain storage transfers, these activities transfer the quarterly balance into 'grain store maximum' rows. Corn may now be sold only from corn actually produced on the farm. Additionally, four 'corn transfer' activities are included in order that produced corn may be transferred into rows where it may be used in livestock production.

By this rather bulky but necessary construction the grain inventory problem is solved in a manner that does not violate reality.
C. Models 3, 4, and 5

These models are duplications of model 2, differences being confined to the land area considered in each. The area of land in model 3 is 1300 acres or 1285 cropping acres. In model 4 the area involved is 1680 acres or 1600 cropping acres. Model 5 has a land base of 2000 acres or 1920 cropping acres. In each of these, plans are obtained for three, four, and five labor units. Since it is assumed that the land area may be purchased within a four mile radius of the present homestead, no attempt to define different soil types and thus different crop coefficients was deemed necessary.

The entire structure of model 5 is presented in computer "print-out" form in Appendix $C$. As can be seen, the size of the model is 95 columns by 51 rows.

In this chapter we have examined and described the construction of the linear programming models used in this study. It now remains to present the results of them.

## VI. PRESENTATION OF RESULTS

Preceding chapters have dealt with problems associated with farm management and have described the framework of programming models used in this study. The empirical findings under various planning situations are now presented. No attempt to draw conclusions will be made in this chapter as those aspects are covered in Chapter VII. Optimum plans for each model are presented in Appendix B and these will be referred to by table number throughout this chapter. In every case the information given by the optimum plan is:

1. The gross return,
2. The net profit (return to entrepreneurship),
3. The grain crops that should be produced and their level of production,
4. The livestock that should be raised and its level of production,
5. The scheduling of grain sales and corn purchases (if required),
6. The quarterly capital transfers,
7. The daily labor hours that must be worked in order that the plan be implimented.
A. Model 1

The results of six separate situations are shown in Table 18. The codes at the top of the table refer to different "right hand sides" of model 1. BJl lists the optimum plans for the 720 acre farm with three labor units while BJ2 gives the optimum plan when an additional labor unit
is hired. BJ5 and BJ6 present optimum plans when corn production is limited to 420 acres for three and four labor units respectively while BJ7 and BJ8 list optimum plans for the farm for three and four labor units when seventy acres of land are diverted into pasture under the Federal Government Feed Grain Program.

The net profit resulting from plan BJ1 is $\$ 29,554$. In this plan 66 acres are used for turkey pasture while the balance of croppable land, 614 acres, is used to raise corn. Turkeys enter the plan at the maximum level of 20,000 birds being limited by presently available turkey facilities. The shadow price on turkey buildings is $\$ 1.43$ per head and sensitivity analysis shows that the shadow price holds up to 23,980 birds. That is, the marginal value productivity of investing in expanded turkey facilities is $\$ 1.43$ per head up to 23,980 birds.

When corn is allowed to freely enter the program it comes in at the maximum possible level after turkey pasture has been deducted. Corn is therefore a feasible and more profitable enterprise than raising soybeans, oats, or diverting land. The shadow price on land is $\$ 77.77$ per acre which holds over the next twenty acres.

Although soybeans have not entered the optimum plan at a positive level they are very closely conpetitive with corn since soybeans are in the basis of the solution at zero level. The sensitivity analysis reveals that the income penalty (the amount that gross returns will decrease) if an acre of soybeans is forced into the plan is $\$ 2.46$ and this penalty
holds up to 54 acres of beans. Just how much more profitable corn production is over other alternatives is shown in Figure 11. The dotted line traces out net profit with three labor units as the maximum corn acreage is reduced and soybeans enter. The reduction of corn to 550 acres allowing 65 acres of soybeans to enter leaves net revenue virtually unaffected lowering it from $\$ 29,554$ to $\$ 29,334$. Livestock activities are unaffected. When corn is limited to 420 acres however, beans occupying the remaining 196 acres, net profit declines to $\$ 26,883$. This fall in profit is a result of the lower returns per acre for soybeans and the need to purchase greater quantities of corn for livestock feed. Also, since labor is limiting in some periods it is not possible for additional livestock to be raised in order to offset the drop in net profit. We notice from Figure 11 that net profit continues to decline monotonically as corn production is curtailed in favor of soybeans. Once diverted land enters at over 70 acres (20 percent) however, net profit descends rapidly to a value of $\$ 22,097$. At this point 210 acres of corn, 264 acres of soybeans, and 140 acres of diverted land are being produced. Thus in this example, the opportunity cost of participating in the feed grain program at the 40 percent level is the difference between net profits of the plans where 614 acres of corn are produced and where 210 acres of corn are produced. This cost is $\$ 7,457$.

Besides turkeys, which we have already mentioned, other livestock that enters plan BJl are raising piglets to sell as feeders (called 'weanlings' on Table 18). The program specifies that 355 head should be raised

for sale in period 1 (December, January, February), that 500 head should be raised for sale in period 2, that 66 should be sold in period 3, and that 138 should be sold in period 4. In period 2 weanlings are raised at their maximum level, the limiting resource being farrowing-nursery facilities. The shadow price on this restraint is $\$ 3.99$ per head. Sensitivity analysis indicates that this value holds up to 1222 head. That is, expanding farrowing facilities so that up to 1222 piglets may be raised per quarter adds $\$ 3.99$ per head to the gross returns (objective function) of the program.

As we might expect labor becomes a restraining resource over spring and summer having a shadow price of $\$ 9.84$ per hour in March-April (Labor 2), $\$ .16$ in May-June, and $\$ 12.60$ in July-August. In this study examination of shadow prices on labor is of limited value in formulating recommendations for two reasons. Firstly, we have assumed, very reasonably, that labor may only be hired in integer units of one man year. Thus we cannot meaningfully make the statement that hiring a man for an hour in March-April will add $\$ 9.84$ to gross returns, since hiring casual labor is not admitted. Secondly, the total available labor hours per period was found by asking the operators "what is the maximum daily hours you are prepared to work per period?" The shadow price on labor is therefore not useful in ascertaining the return to additional hours worked since the operators have previously decided that they are not prepared to work more than the stated maximum. The only usefulness of labor shadow prices is
to indicate to the operators the opportunity cost to them of not working longer hours. From the sensitivity analysis portion of the linear programming printout we find that the shadow price of $\$ 9.84$ in March-April holds for an additional 400 hours. That is, the gross returns (and net profit in this case) forfeited because each labor unit is not prepared to work an extra 2.8 hours per day over this period is $\$ 3936.00$. Similarly in May-June where the shadow price is $\$ .16$ for 63 hours the penalty for not working an extra 25 minutes each per day is $\$ 10.08$. In the months July-August the net profit foregone by not working an additional 33 minutes each per day is $\$ 958$.

As we see from Table 18 slightly less labor is required in some months when we move to plans that have smaller acreages of corn. It is notable however that there is no slack labor over May to August. This is because turkeys remain in the plans at their maximum level and require sizable quantities of labor over that time.

The effect on net profit and optimum plans of hiring an additional labor unit is presented in plans BJ2, BJ6, and BJ8 of Table 18. As can be seen, although the act of hiring another man adds $\$ 8,000$ to fixed costs, the net profit of the plans is greater than that of corresponding three labor unit plans. Comparing BJ1 with BJ2, which have three and four labor units respectively, we find that net profit of BJ1 is $\$ 29,554$ while for BJ 2 it is $\$ 30,350$. That is, if an additional man is hired at a cost of $\$ 8,000$ per year, net profit is estimated to increase by $\$ 796$. Further, daily working hours for all labor are decreased. The solution therefore
indicates that hiring an additional man is a profitable adjustment.
Examining the activities that have entered plan BJ2 we find that with the exception of raising more weanlings and consequently buying more corn, all enterprises enter at the same level as the parallel three labor unit plan. Hiring an extra hand merely adds 375 weanlings to annual hog production.

The solid line in Figure 11 traces out net profit of optimum plans as corn acreage is reduced when four labor units are employed. The vertical distance between this line and the dotted line at any point indicates the marginal profit of hiring an additional man. As the figure attests, the profit margin remains constant regardless of which plan is put into effect. It is therefore always profitable to have four men operating the farm. We may alternatively state that when three labor units are employed the resource labor is limiting and is being spread too thinly over the farm depicted by model 1. Its marginal value product is positive and large. If a fourth labor unit is engaged the marginal value productivity of labor is still positive but of a smaller magnitude. Utilizing four labor units leads to a more optimal farm structure than operating the farm with three.

Another alternative farm structure worthy of consideration is the possibility of cash renting the cropping land in order that the operators may specialize in livestock production. The basic model was altered so that 620 acres of land was rented out at $\$ 50$ per acre. Of the remaining 100 acres, a maximum of 80 acres could be used for turkey production, the
remaining twenty being occupied by hog buildings, sheds, grain bins, and houses. Since the machinery compliment required to operate such a system is considerably less than that required when 620 acres of land are cropped, fixed costs were accordingly adjusted. The results of this model are shown in Table 19, BJIR depicting a situation where three men are employed and BJ2R being where an additional hand is hired.

The net profit when three men are employed is $\$ 23,494-\$ 6,060$ less than plan BJl where 614 acres of corn are raised, but $\$ 2,520$ more than where the operators opt to participate in the Government Grain Program at the fifty percent diversion level.

Table 19 presents the level of activities that have entered the optimal solution. Greater quantities of corn are purchased than in previous solutions but since grain storage is no longer at its maximum in any period, all corn required for livestock production is purchased in period 4 when it is cheapest and is stored until used. In period 1, 327220 pound hogs and 50040 pound weanlings are sold. In period 2 a further 500 weanlings are sold. The activity 'hog expansion $3^{\prime}$ ' enters the solution at 233 head. Hogs raised for sale in period 3 require farrowing space in period 2. Since weanlings completely fill this space it is necessary that the hog expansion activity enter where the returns have been adjusted to allow for the construction of further farrowing space.

Turkeys enter the solution at the maximum level of 20,000 head and turkey expansion, where the costs of enlarged facilities are accounted for, enters at 4,240 head.

As daily working hours indicate, the seasonal demand for labor under this plan is more even than in plans where crops are grown. It is no longer necessary for the operators to work up to eleven hours per day over the spring-summer period.

The effect of hiring an additional hand is shown in BJ2R of Table 19. As with previous situations it is profitable to do this as net profit increases from $\$ 23,494$ with three labor units to $\$ 24,723$ with four labor units.

The only production activity that is altered from BJlR is hog production. The plan specifies that 701 hogs should be raised for sale in period 1.

This concludes the presentation of results of model 1.

## B. Model 2

The optimum results of nine separate situations are presented in Table 20. As with model 1 each situation represents the optimum plans when either different quantities of labor or different maximum corn acreages are placed in the model. In model 2982 acres are available for crop production, the remaining 58 acres being used for yards, buildings etc.

The net profit resulting from plan BO1 where three men are employed is $\$ 44,848$. Corn occupies 892 acres and the balance of 90 acres is utilized as turkey pasture. Neither soybeans, oats, or diverted land enter this solution. Sensitivity analysis indicates that forcing in an acre of soybeans would reduce returns by $\$ 6.02$ for the marginal acre only.

Although the analysis specifies that forcing in an acre of diverted land would reduce returns by a mere $\$ 2.34$ we must ignore this portion of the analysis as diverted land cannot enter until corn production is reduced to below the Federal Government corn base acreage for the farm. This is 491 acres in model 2. The shadow price on oats is $\$ 38.60$ which is constant up to 22 acres of oats. Further, sensitivity analysis reveals that the per acre cost of raising corn (the value in the objective function) may increase by $\$ 3.41$ or decrease by $\$ 308$ before the optimum plan will alter.

As we might expect the shadow price on land is smaller than in model 1 because a larger area of land is being considered. In model 2 the marginal revenue resulting from the addition of an extra acre of land is $\$ 59.80$ and this remains unchanged up to 1037 acres.

The principal livestock raised under this plan is turkeys, entering the solution at 27,250 birds. In addition the plan specifies that 172 weanlings be raised for sale in period 2. With such a small number entering the optimal solution it is doubtful whether the operators would maintain farrowing facilities and a breeding herd merely to produce 172 wean1ings.

In this model the program may select the optimum grain storage capacity (if in excess of 70,000 bushels) for each plan. In BOl the program finds it profitable to purchase grain bins which will hold an additional 41,400 bushels of grain. The penalty for purchasing more than this quantity is 1.6 cents per bushel up to 45,625 bushels whereas the penalty for purchasing less is 1.4 cents on the marginal bushel only. Turning to the corn
merchandizing activities we find that most corn is purchased in period 4 when it is cheapest. Small quantities are purchased in periods 1 and 2 as more storage space becomes available. The balance in storage in period 3 is sold when corn price is highest. This also means that the grain bins are empty going into period 4 so that harvesting and buying new seasons corn can take place.

Since the main production activities of this plan, viz., raising corn and turkeys, are activities requiring spring, summer, and fall labor, we find that labor is virtually idle over the winter months of period 1 , the program indicating that it is only necessary for each hand to work about two hours per day. On the other hand during labor periods 2, 3, and 4 labor utilization is at the maximum allowed having a shadow price of $\$ 30.88$, $\$ 27.57$ and $\$ 6.22$ per hour in labor periods 2,3 and 4 respectively. In model 2 we find that labor has become a far more limiting resource than in model 1 as indicated by the larger shadow prices on labor. In labor 2 alone the shadow price of $\$ 30.88$ is constant over the next 153 hours. That is, the operators forfeit $\$ 4724$ by not working for an additional 1.1 hours each per day during the months March and April.

Plans BO7 and B14 illustrate how the basic three labor unit plan alters when corn is limited to 600 acres (in the case of BO7) and when corn is limited to half of the corn base acreage the other half being placed in diverted land, (in the case of plan Bl4).

In BO7 net profit has decreased by $\$ 2,355$ to $\$ 42,493$. As Table 20
shows the principal difference is the substitution of soybeans for corn, the absence of weanling production, and the inclusion of the fattening of 78 feeder hogs.

In plan B14 net profit has crashed to $\$ 34,143$, a drop of $\$ 10,705$ compared to BO1. In this plan 227 acres of corn, 402 acres of soybeans, 264 acres of diverted land, and 89 acres of turkey pasture are produced. As a consequence more corn is purchased and less sold in order to feed 27,100 turkeys and 406 feeder hogs.

The dotted line of Figure 12 traces out the decline in net profit as corn production is reduced. The slope is almost constant from 892 acres of corn down to 393 acres where twenty percent of the corn base acreage is placed into diverted land. The decision to participate further in the land diversion program involves a more than proportionate drop in profit.

Returning to Table 20, by observing columns B02, B08, and B15, we see the effect of hiring an additional hand. Perhaps the most noticeable difference is the increase in net profit of around $\$ 20,000$ over the corresponding three labor unit plan. For BO2 net profit is $\$ 64,897$. Turkeys have entered at the maximum level of 43,000 birds requiring 142 acres of pasture. Corn occupies the remaining 840 acres. As with BO7 weanlings for sale in period 2 come into the solution in this case at a level of 143 head. In addition the program specifies fattening 165 feeder hogs for sale in period 1. In plan BO8 where total corn acreage is limited to a maximum of 600 acres net profit has declined from $\$ 64,897$ to $\$ 62,845$. Soybeans have substituted for corn. Since some labor is freed when this substitution occurs a greater quantity of feeders 1 enter the solution

(213 head) and 67 feeders for sale in period 4 also come in. Turkeys remain at the maximum level.

Referring to Figure 12 we note from the solid line that the decrease in profit as corn acreage is reduced is at the same rate as for the three labor unit case, being approximately constant down to 393 acres where twenty percent of the corn base acreage is diverted then falling at a rather steeper rate as the option to participate in land diversion at greater than twenty percent is taken.

The upper line of Figure 12 specifies the net profit at various corn acreages when five men are employed by the farm-firm. As we note the resultant increase in net profit by hiring an additional hand is $\$ 12,500$. The addition to net profit by having five men operate the farm-firm depicted by model 2 rather than three men is $\$ 33,530$.

Clearly the marginal value product of hiring extra labor is very large in this model but is, as we might expect, diminishing as extra units of labor are added. This is indicated by the smaller vertical distance between four and five labor units than between three and four labor units. It is extremely profitable for the operators to hire two full time men and the marginal value product of the last unit is still positive and large. We can therefore profitably hire more labor than this but since we can only hire labor in integer quantities and since we have not considered the case where a sixth man is hired, we cannot tell where the marginal value product of labor, expressed in net terms, equals zero.

Plans B03, BO9, and B17 of Table 20 identify the level at which activities should be operated if the plan is to be practiced. We notice that the basic difference over previous plans is that larger numbers of weanlings are produced. Working hours have also been reduced in peak periods and increased in slack periods so that seasonal labor demand is more even. Labor is still scarce and therefore limiting in two periods. In period 2 labor has a shadow price of $\$ 40.16$ per hour which is constant over the next 102 hours worked, and in labor period 4 the shadow price of labor of $\$ 9.67$ per hour hold over the next 181 hours.

## C. Model 3

The optimum results of nine separate plans are presented in Table 21. As with previous models each plan lists the optimum activity level when either different quantities of labor or different maximum corn acreages are placed in the model. In model 3 the land area considered is 1390 acres, 1285 acres being available for crop production.

The net profit resulting from plan B10 where three men are employed is $\$ 40,042$. In this plan corn enters at 594 acres, 592 acres being allocated to corn grain production and two acres being used for corn silage production. Soybeans which require less labor per acre than corn come into the plan at 572 acres. Since labor is limiting, the program finds it profitable to reduce the acreage of corn and raise larger acreages of soybeans. Turkey pasture occupies 70 acres and the balance of 49 acres goes into diverted land.

For the first time in these models cattle have entered the solution. We find that the activity 'yearlings 42 A ' has come in at 36 head. This number is so small that it would be difficult for a farmer to justify the overheads of a system designed to fatten 36 head and we would probably find that an operator attempting to implement this plan would ignore the cattle raising activity adjusting the rest of his plan accordingly. The only other livestock that has entered are turkeys. The plan indicates that 21,264 head should be raised.

Because of the large acreages of soybeans and corn,grain storage is insufficient and the plan specifies that bins equivalent to 26,872 bushels of storage capacity be purchased.

Labor is a very limiting resource over the period March through August having a shadow price of $\$ 30.39$ in labor 2, $\$ 27.42$ in labor 3, and $\$ 9.28$ in labor 4. Land is also restrictive having a shadow price of $\$ 57.71$ on the next acre.

In plan BO1 diverted acres were excluded from entering the solution and corn was free to enter at up to 1285 acres. As Table 21 indicates corn production falls from 594 to 442 acres, soybeans increase by 200 acres, turkey production decreases marginally by 884 birds, and net profit falls by $\$ 1,568$. Plan BO1 would probably be rejected by a farmer since not only is net profit smaller but a greater acreage of crops using slightly more labor is required.

Plan Bl4 shows the optimum level of activities when fifty percent of the corn base acreage is forced into the plan. Net profit has declined by $\$ 8,287$ compared to plan Bl0. This is because the profitable activity
of corn production has been curtailed by 273 acres and soybeans have been unable to increase because of the extra land in diverted pasture. Figure 13 (dotted line) indicates the magnitude of the decrease in net profit as corn acreage is reduced.

In plans B02, B08, and B15, four units of labor are employed. Since more labor is now available the high profit but high labor requiring activities of growing corn and raising turkeys are expanded over the three labor unit plans. In BO 2 corn production has increased to 1164 acres and turkey raising has jumped to 36,700 birds boosting net profit to $\$ 66,228$ a net increase of $\$ 17,754$ over the corresponding three labor unit plan. That is, investing $\$ 8,000$ in hiring an extra man has netted the farm-firm $\$ 17,754$. No soybeans are produced nor land diverted in this plan. As with previous plans we find the grain merchandizing activities operating in such a manner that all bins are filled with grain, either produced or bought, in period 4. As livestock consume grain in successive periods so it is replaced by bought corn until period 3 when all that is remaining is sold leaving the bins empty for the new season's production.

Eleven yearling steers and 304 'weanlings 2' are raised under this plan. Again, a farmer implementing plan $B 02$ would probably ignore the eleven head of cattle since it is such a small number and would not warrant the fixed investment in facilities required.

Labor is also restrictive in this plan in three labor periods having a shadow price very similar to that of plan B10. In labor 2 the shadow price is $\$ 30.87$ for the marginal hour of labor worked, in labor 3 the
shadow price is $\$ 27.34$, while in labor 4 the shadow price is $\$ 6.35$. Somewhat more hours of work over Fall and Winter are required in this plan compared to plan Blo.

Plans BO8 and B15 identify changes in profit and optimum activity levels when corn acreage is reduced and when diverted land is forced into the program. In plan BO8 corn acreage is reduced to 800 acres, the balance being taken up by soybeans and turkey pasture. Turkey production has increased by 850 birds, weanlings 2 have left the plan and 133 feeders to be raised for sale in period 1 have entered. Net profit has fallen from $\$ 66,228$ (in BO2) to $\$ 63,540$.

Fifty percent of the corn base acreage is placed into diverted land under the Federal Government Feed Grain Program in plan B15. This means that corn may only enter at a maximum of 321 acres while soybeans occupy 521 acres and turkey pasture requires 121 acres. Feeders 1 have increased to 270 head and feeders 4 have entered at 250 head. Turkey production has declined back to the BO2 plan level of 36,700 birds.

Because of the greatly reduced corn acreage and the impossibility of fully compensating for this reduction by increasing other activities, net profit under plan B15 has subsided to $\$ 51,930$. The solid line of Figure 13 illustrates the interrelationship between net profit and total corn production when four labor units are employed. As may be seen the function decreases approximately monotonically from 1200 acres of corn down to 500 acres (where twenty percent of the corn base acreage is diverted) then falls at a greater rate as the option to participate further in the feed grain program is accepted.

The hiring of a fifth labor unit adds approximately $\$ 15,500$ to the net profit of equivalent four labor unit plans, as shown in Figure 13. Since the marginal net profit between four and five labor unit plans is smaller than that between three and four labor unit plans (as found by the vertical distance between net profit lines at any point) we know that we are in a region of diminishing marginal productivity of labor. This is true since labor is the only parameter that has been altered. Its marginal productivity is still positive and large however even at the highest level we have considered.

Plans B03, BO9, and B17 of Table 21 specify the optimum activity levels for various corn acreages when five labor units are engaged. The net profit resulting from plan B03 is $\$ 81,688$ which is generated from the production of 1139 acres of corn grain, 4 acres of corn silage, 43,000 turkeys, 1500 weanlings for sale in period 2 , and 53 head of 'calves 22A'. The plan also indicates that a further 79,000 bushels of grain storage should be purchased.

With greater availability of labor and therefore the opportunity to produce more corn and turkeys, the shadow price of land has increased over earlier plans of model 3 and now stands at $\$ 74.30$ on the marginal acre. Also labor is now only restrictive in two periods. In labor period 2 (March and April) the shadow price of labor is $\$ 40.12$ per hour while in labor period 4 (July and August) it is $\$ 10.07$.

Plans B09 and B17 indicate that as corn acreage is reduced, being replaced by diverted land and soybeans, net profit declines - down to

$\$ 71,064$ in plan B17. Turkey production is at its maximum and therefore cannot increase as more labor becomes available. Weanlings 2 have entered at a reduced level of 561 head and 'steers $42 \mathrm{~B}^{\prime}$ have come in at a practicable level of 348 head. Since less corn is being raised the need for grain storage is less so that by plan B17 it is not necessary to purchase any additional grain bins and bins reach maximum capacity only in period 1 . We shall now continue to an examination of the results of model 4.

## D. Model 4

Table 22 details the optimum results of nine separate plans. As with previous models each plan lists the optimum activity level when either different quantities of labor or different maximum corn acreages are placed in the model. In model 4 the land area considered is 1680 acres, 1600 acres being available for crop production.

The net profit resulting from plan BOl where three men are employed is $\$ 28,168$. In this plan diverted land is excluded from entry but corn may enter up to the full acreage available. As we see the only corn produced in plan BO1 is ten acres for use as silage. Instead of corn being the principal crop soybeans enter at 1557 acres. Turkey production is at a low level - 9,910 birds - and the only other livestock coming into the plan is 168 yearlings 42A. Obviously labor has become extremely restrictive in this plan as corn and turkey production (high labor requiring activities) are far less than in model 3. Indicative of the scarcity of labor is the shadow price on labor. In labor 4 the shadow price is $\$ 97.07$ on
the marginal hour, and $\$ 15.19$ in labor 2. Contrarily, the shadow price on land is a mere $\$ 22.25$ indicating that because labor is so limiting an additional acre of land is not a useful investment. (Although purchasing an additional acre of land would add $\$ 22.25$ to gross returns it would also add in excess of $\$ 42.00$ to fixed costs so that a net loss of approximately $\$ 20.00$ would result from the transaction).

In plan Blo up to twenty percent of the corn base acreage of the farm may be placed in diverted land. When the plan finds it possible to do this as in plan Blo net profit increases by $\$ 6,316$ to $\$ 34,484$. Now corn grain production is at 291 acres, diverted land at 160 acres, soybeans occupy 1096 acres and turkey pasture uses 51 acres, allowing turkey production to increase to 15,580 birds. The eighteen yearlings 42 A which are specified in the plan may be best excluded in practice for reasons given previously. Plan Blo of model 4 shows that only when acreage is so large as to make existing labor very scarce, is it profitable to participate in the feed grain program. All previous plans have recorded a loss in net profit when diverted land has been forced into the solution.

If fifty percent participation in the feed grain program is forced into the program as in plan B14 then profit falls compared to when twenty percent participation is chosen. Plan B14 gives a net profit of $\$ 28,789-$ $\$ 5695$ less than plan B10. When such a large area of land ( 400 acres) is diverted as in B14 then sufficient labor is then available to allow a matching 400 acres of corn to be grown. The remaining land is used for soybean production (748 acres) and turkey pasture (52 acres). Cattle have
left the plan entirely and have been replaced by 214 feeder hogs which are scheduled for sale in periods 1 and 4.

In this plan the shadow price on land has increased to $\$ 65.92$. For labor which is restrictive over spring and summer the shadow price is $\$ 66.49$ on the marginal hour on labor 2, $\$ .40$ on labor 3 , and $\$ 5.92$ on labor 4. The labor demand is very seasonal in this plan being at its peak over spring and summer, about six hours per day in fall, and averaging less than two hours per day in winter.

We note that the net profit of model 4 when three labor units are employed is less than that for model 2 and model 3 where smaller acreages were involved. The reason this is the case is because of the large fixed costs associated with owning the extra area of land and the inability of three labor units to farm it sufficiently intensively under the assumed technology and prices. That is, the resource labor is being spread too thinly over the land area in model 4 where only three men are employed. Plans BO2, B11, and B15 indicate the changes in optimum plans that occur when a fourth hand is hired. Net profit actually doubles going from $\$ 28,168$ in BO1 to $\$ 59,974$ in BO2. This serves to illustrate the high marginal productivity of additional labor and how restrictive labor must be in the three labor unit plans of model 4.

In BO2 corn production is at 823 acres all except four acres being for corn-grain production. Soybeans occupy 678 acres and turkey pasture fills the remaining 99 acres. Turkey production has now expanded to 30,000 birds and the program states that 66 head of yearlings 42 A should be
fattened. Since a greater quantity of corn is now being produced it is also profitable to purchase a further 59,477 bushels of grain storage. As with previous plans of model 4 the shadow price on labor is very high. In labor 2 the shadow price is $\$ 21.53$, in labor 3 it is $\$ 8.23$, while in labor 4 it is $\$ 63.25$ per hour. With such high shadow prices it is evident that labor is still very obstructive to greater profit even though an extra hand has been hired. This evidence is confirmed in plans B03, B16, and B17 where a fifth permanent hand has been employed. The effect of this is to boost net profit of the farm-firm depicted by model 4 to $\$ 85,250$ in the case of plan BO3 - an increase of over $\$ 25,000$ compared to plan BO2. The marginal productivity of labor is still obviously very high although we are in a region of decreasing marginal productivity.

Plan BO3 specifies that 1452 acres of land should be used to raise corn grain, five acres should be for corn silage production, and 142 acres should be used for turkey pasture. Soybeans and diverted land do not enter although beans are close to entering as the penalty for producing an acre of them is only $\$ 2.04$. Turkey production reaches its maximum of 43,000 birds and weanlings 2 , the only other livestock in the plan, enter at 433 head.

With five workers, labor becomes limiting in only two periods and with smaller shadow prices than previous plans of model 4. The shadow price in labor 2 is $\$ 33.12$ and in labor 4 is $\$ 16.27$.

Since labor was spread so thinly in plan BO2 an additional acre of land is not as valuable as in plan BO3 where five labor units are available. The shadow price of land in BO2 is $\$ 33.86$ while in BO3 it has risen to \$70.69.

Figure 14 illustrates the interaction of net profit and corn acreage in model 4. The solid line indicates that net profit falls rather rapidly once corn acreage is reduced below 1000 acres in the five labor unit case. Only three points are given for the four labor unit case as they extend over the total variability of all four labor unit plans. Again, profit falls as corn acreage declines. The vertical distance between the two lines gives the marginal net profitability of hiring an extra hand.

This concludes the presentation of the results of model 4. We shall now examine the results of model 5 .

## E. Model 5

The optimum results of nine separate plans of model 5 are given in Table 23. As with prior models each plan lists the optimum activity levels when either labor or maximum corn acreage is varied. In model 5 the land area considered is 2000 acres, 1920 acres being available for crop production.

Plans B10, B12, and B14 list the optimum activity levels of the 2000 acre farm when three men are employed. Net profit of these plans varies from $\$ 26,688$ to $\$ 30,250$. We would expect the net profit of these plans to be less than in models 2,3 , and 4 because in model 4 , which has less land than model 5, net profit had begun to decline because of limiting labor and large fixed costs. That is, under the assumed technology, prices, possible farm activities, and available labor, we have exceeded the

optimal farm size. Since this is the case, the plans presented in B10, B12, and B14 do not represent advisable proposals in terms of practical farm recommendations and will therefore not be studied further at this juncture.

In plans B02, B11, and B15, where four labor units are utilized, net profit has almost doubled from previous plans of model 5 ranging from $\$ 48,073$ in plan B15 to $\$ 59,071$ in plan Bll. The results of these plans, listed in Table 23 indicate that it is profitable to participate in the feed grain program up to the twenty percent diversion level although diverting more land than this involves some decrease in profit. Examining plan Bll we find that 760 acres of corn grain and one acre of corn silage is raised. Turkey pasture uses 84 acres while soybeans is the predominant crop requiring 882 acres. Diverted land enters at 192 acres ( $20 \%$ of the corn base acreage). Turkeys are the only livestock raised entering the program at 25,600 head. The twelve head of cattle that come in are best ignored for reasons given previously. Because of the large area in corn and beans it is profitable for the plan to purchase 60,347 bushels of additional corn storage bringing the farm-firms total storage capacity up to 130,000 bushels. The program specifies that corn remaining in period 3, approximately 84,000 bushels, should be sold before the end of period 3 while corn should be bought in periods 1,2 , and 4. The soybeans are stored for about nine months before being sold in period 3 , while the 4000 bushels of oats harvested from turkey pasture are stored for sale in period 1.

Labor is the most limiting factor becoming restrictive in three labor periods. In labor 2 the shadow price of labor is $\$ 21.52$ which is constant over the next 300 hours. The shadow price on labor 3 of $\$ 8.23$ holds over the next 13 hours while in labor 4 labor has a very large shadow price of $\$ 63.25$ on the marginal hour only.

The program indicates that the addition of land is not profitable. The shadow price of $\$ 33.86$ on land which is constant on 45 additional acres, is insufficient to cover the fixed costs associated with land ownership. (If land is purchased at $\$ 700$ per acre the annual interest charge on an acre at six percent is $\$ 42.00$ ). In fact with the present resource structure we have an excess of land. The shadow price indicates that if we deduct an acre of land from the plan the gross returns (objective function) will be decreased by $\$ 33.86$. This penalty remains true down to 1425 acres. However we have seen that an acre of land contributes in excess of $\$ 42.00$ to fixed costs. Thus decreasing the land area of this plan by one acre increases net profit by at least $\$ 8.14$ and this is constant until the land area has been reduced by more than 495 acres (1920 acres minus 1425 acres).

Plans BO3, B16, and B17 tabulate optimum activity levels when five workers are engaged. The net profit of these plans varies from $\$ 72,036$ to $\$ 83,535$ depending on the area of corn raised. Net profit has increased by approximately $\$ 25,000$ over the four labor unit plans indicating the gross shortage of labor experienced in these plans.

In plan BO3 labor is still not sufficiently abundant to allow the two
most profitable but most labor intensive activities of corn and turkey raising to enter the plan at their maximum level. Corn comes into the plan at 1188 acres of corn grain and 4 acres of corn silage while 39,378 head of turkeys are raised. Soybeans occupy the remaining 598 acres. Besides turkeys the only livestock raised in this plan are 74 yearlings 42 A . With the large production of grains the program finds it profitable to more than double existing grain storage by adding bins which have a capacity of 102,000 bushels. This increases the total grain storage capacity of the farm-firm depicted by model 5 to 172,000 bushels.

Labor remains limiting in these plans over spring and summer. The shadow price on labor 2 is $\$ 21.52$ and sensitivity analysis reveals that this is constant over the following 383 hours. In labor 3 the shadow price of $\$ 8.23$ holds over 82 hours and the shadow price on labor 4 of $\$ 63.25$ is stable up to an extra 65 hours. From this result we thus might conject that under the conditions assumed in this model five labor units are suboptimal on a farm of 2000 acres. Alternatively we may state that the optimum sized farm for five labor units is less than 2000 acres. Our conjecture is confirmed when we examine the shadow price on land. As with plan Bll the shadow price of land is $\$ 33.86$ which we have shown represents a penalty in excess of $\$ 8.00$ per acre for having too much land. The shadow price remains constant over 138 acres indicating that we have at least 138 acres too many. That is, the marginal productivity of land has been driven below its price. Without recomputing the problen we cannot tell exactly how oversized our farm in model 5 is.

Plans B16 and B17 show how the optimum plan alters as corn acreage is reduced and diverted land forced in. Net profit subsides to $\$ 72,036$ in Bl7 as forty percent of the corn base acreage is diverted. Soybeans increase by 200 acres and turkeys increase marginally. In addition feeder hogs begin to enter the plans reaching levels of 225 feeders 1 and 217 feeders 4 in plan Bl7. Since less corn grain is being raised the need for additional grain storage diminishes so that only 35,000 extra bushels are specified for B17.

Figure 15 illustrates the effect of corn acreage on net profit. With the exception of the five labor unit function the relationships shown do not bear the same resemblance and general shape as similar functions of other models. The reason that this is so is because the land area is too large in proportion to the available labor to be completely utilized in corn production.

In this chapter we have presented the optimum results of models 1 through 5. As mentioned in the preamble to this chapter, with the exception of emphasizing some obvious points no attempt to make recommendations, draw inferences, or reach conclusions has been made. These aspects will be covered in the subsequent chapter.

 corn production, with ;
3 labor units -...--,
4 labor units_, and
5 labor units_-_-
VII. RECOMMENDATIONS AND CONCLUSIONS, DISCUSSION, AND SUMMARY

In this chapter we shall attempt to make recommendations and draw conclusions from the results presented in Chapter VI. We shall return to model 1 and work through to model 5 bringing each model together in a comparative static framework in order to approximate a growth situation.

## A. Recommendations and Conclusions

This study is an attempt to formulate optimum resource use and activity levels for a specific farm-firm under stated assumptions regarding farm size and labor utilization. For this reason it is pertinent that the results be presented as a series of general recommendations which entrepreneurs of the farm-firm may use as a basis on which to make future decisions concerning the growth or expansion of their farm-firm.

From model 1 we have seen that it is possible and profitable for the operators to raise corn on a continuous basis up to the limit of land available after turkey pasture has been deducted. Although the most profitable plan is one where 614 acres of corn and 66 acres of turkey pasture are produced, Figure 11 indicates that the loss in revenue if limited quantities of soybeans are planted is not large. The recommendation therefore is that if maximum profit is desired the operators of the 720 acre farmfirm depicted by model 1 should produce corn to the maximum acreage possible after 66 acres of turkey pasture has been sown. If, because of adverse weather or the emergence of a pest problem, the full 614 acres
of corn cannot be planted then the loss in revenue caused by a reduction of 120 acres of corn is not large - about $\$ 700$ net. If the operators desire to produce more soybeans than this or participate in the feed grain program then they must be prepared to accept the drop in net profit resulting from such sub-optimal plans as shown in Figure 11.

A further recommendation that may be made from model 1 is that regardless of the plan implemented it is only marginally profitable to hire an additional hand. The gross margin resulting from taking this action is approximately $\$ 8,800$. In all models we have assumed that the fixed cost of hiring a permanent man is $\$ 8000$, so that in model 1 the marginal net profit derived from utilizing an extra hand is only $\$ 800$. To the extent that the entrepreneurs of the farm-firm (a) can hire a permanent hand at a smaller or greater price, (b) prefer to have more leisure time letting the hired hand do more work, and (c) are prepared to assume the responsibility of supervising a hired man, so their decision on this matter will be made.

The results of model 2 show that expansion of the farm-firm by the aquisition of an additional half section of land is a very profitable adjustment. From Figure 16 we find that with three labor units net profit has increased by $\$ 15,295$ over model 1 to $\$ 44,848$. The figure also indicates that under the assumed conditions the land base should not be expanded beyond 1040 acres. In other words, optimum farm size when three men are employed under the technology, prices, resources, and possible activities assumed here is in the order of 1040 acres. If the farm-firm

attempts to expand beyond this by merely increasing its land base then it will experience a decrease in net profit.

With regard to activity levels of three labor unit plans of model 2 we can make the same recommendations as for model 1 . After excluding 90 acres of land for turkey pasture the balance of land should be planted in corn. The forfeit for not doing this is relatively small however as Figure 12 attests. If corn production is decreased by 300 acres net profit falls by only five percent to $\$ 42,493$.

In model 2 there is no question as to the advisability of hiring a fourth hand. Gross profit increases by $\$ 28,000$ over three labor unit plans. In net terms if hiring an extra hand costs $\$ 8,000$ as assumed here, then the increase in net profit is $\$ 20,000$. The magnitude of marginal net profit when an extra labor unit is added is indicative of the suboptimal labor use in the three labor unit plans of model 2. It is suboptimal in the sense that its marginal value product is extremely high.

As Table 20 indicates, we can recommend that a fifth labor unit be added to the farm-firm since the incremental net profit from doing so is $\$ 12,500$. Although the marginal value product of labor has decreased it is still positive and far exceeds its price. That is, we have not yet driven the marginal value product of labor to its optimum level - where it equals the price of hiring an additional hand. When the farm-firm has five men employed on it net profit rises to $\$ 77,379$.

Previous recommendations of model 2 concerning activity levels remain true in the case of five labor units. The most profitable plan is where the maximum number of turkeys are produced and the maximum acreage of corn
is raised. The opportunity cost of not adhering entirely to corn but planting beans or participating up to twenty percent in the feed grain program is not large as is shown in Figure 12. The operators may prefer to accept the small decrease in profit in order to diversify their operations.

The decision of the entrepreneurs of the farm-firm to purchase another 320 acres to bring total acreage up to 1360 acres as has been done in model 3, must be accompanied by the decision to employ at least four men. As Figure 16 shows, to attempt to operate a farm of 1360 acres with only three men under present technology would reduce net profit. Figure 17 however indicates that net profit will increase from $\$ 64,897$ in model 2 to $\$ 66,228$ in model 3 when four men are employed. Figure 17 also indicates that a farm of 1360 acres gives the maximum net profit of all farm sizes considered under the assumptions of the models. That is, the optimum farm size under technology, prices, resources, and activities assumed in the study for a four man operation is around 1360 acres. If the entrepreneurs attempt to expand the land base only beyond this point they will experience a decrease in net profit.

The optimum activities of four labor unit plans of model 3 are essentially the same as model 2. Turkeys enter at 36,000 birds and corn occupies the remaining land. The opportunity cost of substituting soybeans for corn is relatively small being only $\$ 2,800$ or four percent if 364 acres of soybeans replace corn. If the operator wishes to divert twenty percent of his corn base acreage then the opportunity cost compared to planting all corn is $\$ 6,400$, or a decrease of ten percent.


The results of model 3 listed on Table 21 indicate that it is very profitable to hire a fifth permanent worker. By doing so net profit of the farm-firm represented by model 3 is increased from $\$ 66,229$ to $\$ 81,688$ a net increase of $\$ 15,440$.

With respect to activity levels of model 3 when five labor units are employed, the same recommendations as for four labor unit plans are true. Corn and turkeys remain the most profitable activities. If the operators wish or find it necessary to plant soybeans then the decrease in net profit is of a small magnitude - reducing corn by 343 acres and replacing it with soybeans decreases net profit by less than $3 \%$ to $\$ 79,316$. If twenty percent of the corn base acreage of the farm is diverted the decrease in profit is somewhat larger being eight percent or \$3,500.

We have already seen from Figures 16 and 17 that net profit is declining when three or four labor units are employed on defined farms larger than 1360 acres. Thus in model 4 where farm size is 1680 acres the only profitable labor combination considered is five men. If the operators desire to own 1680 acres they will require at least five men to operate the farm-firm at a level more profitable than that depicted by model 3 . Even so, net profit has only increased marginally by $\$ 3,500$ to $\$ 85,250$. This represents a mere four percent increase in net profit.

As Figure 14 indicates previous recommendations with respect to corn acreage remain in force. The most profitable plan is where the highest proportion of corn is planted. As corn acreage declines net profit falls.

Model 5 represents a farm of 2000 acres. Figure 18 indicates that if we attempt to expand to this farm size under the assumptions and with five or fewer labor units, net profit will decline in comparison to smaller operations. Since we are only considering five, four, or three labor units we cannot recommend that under the present technology a farm of this size be operated. Figure 18 reveals that the optimum farm size with five men and other assumptions made is in the vicinity of 1680 acres.

As an overall recommendation for profit maximization we would advise the operators that subject to present technology, prices, resources, and activity possibilities considered in this study, the most profitable structure is one where five units of labor resource are used to operate a land base of around 1680 acres in the manner specified in plans BO3, B06, or B16 of model 4.

## B. Discussion

In the United States, the objective of farm management and production economics research is typically stated in terms of developing information useful to decision making by individual farmers (1). This study claims to meet that objective by providing advice, based on a particular entrepreneur's aims, pertaining to the optimization of a farm-firm. We have studied several alternative static models and from these have made recommendations concerning the optimum combination of resources with activities to give a restrained profit maximization solution. We have attempted to incorporate non-economic aspects of the entrepreneurs objectives by limiting the number of hours that the operators may work per week and by the

maximum levels set on several activities.
In order that we keep the results of this study in correct perspective it may be helpful to restate the assumptions in explicit form.

1. Because of the linearity assumption no consideration has been given to rising costs and time associated with travelling distances between land holdings as farm-firm size increases. The magnitude of these costs obviously depends on the distance between blocks of land operated by the farm-firm.
2. We have assumed that land added to successive models is immediately available in the right quantity and correct locality. This assumption is probably reasonable when we consider that the area of land within a four mile radius of the farm-firm headquarters is 25,600 acres and that over 1000 acres of that has been for sale over the past six months. ${ }^{1}$
3. The linear programming models used in this study are deterministic. Prices and yields are given and assumed to be known with certainty.
4. As a series of comparative static models, the study fails to take account of possible technological advances that will inevitably occur in future years. The models merely portray one year in a farm-firm's operation. They are static equilibrium models. The use of a dynamic model to trace an optimal expansion path was not employed for two reasons. Firstly, in a real world situation it is only possible for an entrepreneur to purchase additional land as it comes onto the market. The entrepreneur

[^7]must then usually purchase the farm as a whole entity. It is therefore not realistic to ask a dynamic program "when and how much additional land should be purchased." Secondly, given the fact that the farm-firm being studied does not face a capital limitation problem, if it is profitable to add land and improvements to the operation then a dynamic program would probably specify that the changes be made immediately. For these reasons static models were used.

Glenn Johnson wrote that "Static economics defines the problem of managing a farm as dealing essentially (1) with resource combinations, (2) with enterprise combinations, and (3) with levels of input and, hence, of output. As the academician looks at the management process in operation on farms he realizes that the list of problems solved by static economics is far too narrow" (31, p. 445). This study succumbs to Johnson's criticism but we defend the methodology used by asserting that the results of the study go far in aiding the entrepreneurs of the farm-firm to make knowledgeable decisions. The study makes no claim to interdisciplinary breadth which we saw from Chapter I is required to support the increasingly broad concept of management, but rather claims to have answered specific questions regarding profitable adjustments of the farm-firm. As such the production economics approach used here has surely contributed to the management of the farm-firm and may represent a small but perhaps significant step in the extension of production economics principles from their "practical application" to "commercial adoption."

## C. Summary

The first chapter of this study dealt with the role of farm management and management decisions in successful farming. We mentioned the complexity of the entire decision making process and pointed out that social scientists, until recently, have had little success in faithfully simulating decision processes in mechanistic models. We then suggested linear programming as a tool available to economists which is capable of overcoming some of the difficulties associated with combining resources and enterprises.

After defining the objectives of the study and describing the present farm-firm structure, we continued to review four production economics principles as applied to linear programming and examine the technique, model, and methodology of linear programming.

In Chapter $V$ the models used to depict five farm-firm situations were described. We saw how the program was constructed to handle the problem of varying returns on diverted land, and how the grain inventory problem was integrated with the general model to give a coordinated solution.

The results of the models were presented in Chapter VI and the implications of them were given in the first part of Chapter VII. Results showed that a considerable increase in profit was possible in model 1 (720 acre farm) by increasing corn production. From a net profit of \$7,750 under present production patterns of the farm-firm studied, the potential increase in net profit by reorganizing activities within present resource restraints to include more corn and turkeys, is in the order of
$\$ 20,000$. Model 1 further showed that the addition of a hired man increased net profit marginally (only $\$ 800$ ).

Other models confirmed the finding of model 1 that corn and turkey production were the most profitable enterprises and where not restrained by labor the program specified that they be produced at their respective maximum levels. Only when labor became severely limiting (such as when three labor units were employed on a 2000 acre farm) did it become profitable for the farm-firm to participate in the Federal Government Feed Grain Program by diverting land out of corn production.

As farm size increased the models showed how marginal net profit from hiring extra labor increased. In all models which had a land base of 1040 acres or greater it was profitable to hire two extra labor units bringing to five the total number of men employed on the farm-firm.

Finally, the results of the study showed that under the activities, restraints, and coefficients considered, optimum farm size when three labor units are employed is in the vicinity of 1040 acres. When four labor units are utilized optimum farm size increases to approximately 1360 acres, and when a fifth man is engaged optimum farm size is in the order of 1680 acres. In Chapter VII we returned to review and conclude the objectives of the study.

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## X. APPENDIX A

Table 4. Tractor operating costs (38)

| Tractor sizeFuel con- <br> sumption <br> per hour | Fuel <br> cost <br> per hour | Oil con- <br> consumption <br> per hour | Oil <br> cost <br> per hour | Total operating <br> cost <br> per hour |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| $55 \mathrm{~h} \cdot \mathrm{p}$. deisel | 3.3 | $\$$ | gallons | $\$$ | $\$$ |
| $85 \mathrm{~h} \cdot \mathrm{p} \cdot$ deisel | 4.5 | .544 | .008 | .013 | .557 |
| $115 \mathrm{~h} \cdot \mathrm{p}$. deisel | 5.8 | .743 | .01 | .016 | .759 |

$a_{\text {Based }}$ on the tractor working at $62 \%$ of its maximum 1 oad .
b Based on a cost of $\$ .165$ per gallon for deisel. $^{\text {Bas }}$.
${ }^{c}$ Based on a cost of $\$ 1.60$ per gallon for lubricating oil.
Table 5. Cropping machinery: capital requirements, useful life, and annual fixed costs (as reported

| Machine | Replacement cost | $\begin{gathered} \text { Life } \\ \text { (years) } \end{gathered}$ | Annual depreciation | Repair cost ${ }^{\text {a }}$ | Taxes and insurance ${ }^{b}$ | Total fixed costs |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Tractor (110 h.p.) | \$6,000 | 8 | \$750 | \$180 | \$120 | \$1, 050 |
| Tractor ( $60 \mathrm{~h} \cdot \mathrm{p}$. | 5,000 | 10 | 400 | 120 | 80 | 600 |
| Truck ( $2 \frac{1}{2}$ ton) | 2,000 | 8 | 250 | 60 | 40 | 350 |
| Truck ( $3 / 4$ ton) | 2,500 | 6 | 416 | 75 | 50 | 541 |
| Feed carrier | 600 | 20 | 30 | 18 | 12 | 60 |
| Plow (8 bottom) | 2,000 | 18 | 111 | 60 | 40 | 211 |
| Spring tooth harrows $(30 \mathrm{ft})$ | 540 | 18 | 30 | 16 | 11 | 57 |
| Spike harrows (30 ft) | 108 | 18 | 6 | 3 | 2 | 11 |
| Sprayer | 425 | 15 | 28 | 13 | 8 | 49 |
| Mower | 600 | 18 | 33 | 18 | 12 | 63 |
| Rotary shredder | 690 | 6 | 6 | 20 | 14 | 40 |
| Side rake | 600 | 12 | 50 | 18 | 12 | 80 |
| Discs (21 ft) | 1,500 | 10 | 150 | 45 | 30 | 225 |
| 2 augers (40 ft) | 540 | 18 | 30 | 16 | 11 | 57 |
| Rotary hoe | 1,160 | 8 | 144 | 36 | 23 | 203 |
| Combine (6 row) | 5,600 | 6 | 934 | 168 | 112 | 1214 |
| Elevator ( 52 ft ) | 1,040 | 8 | 130 | 30 | 20 | 180 |
| Spreader (manual) | 480 | 16 | 30 | 15 | 9 | 54 |
| Corn planter (6 row) | 2,640 | 10 | 264 | 78 | 52 | 394 |
| Total | 33,023 |  |  |  |  | 5439 |
| Av. value ${ }^{\text {c }}$ | 16,511 | 5\% inte | $t=\$ 825$ |  |  | 825 |
| Total annual fixed costs including interest on capital |  |  |  |  |  | \$6264.00 |

[^8]${ }^{\mathrm{b}}$ Taxes and insurance calculated as $2 \%$ of replacement cost.
${ }^{\text {c }}$ Average value is $50 \%$ of replacement cost.
Table 6. Variable costs of crops (per acre) $1968^{\text {a }}$

| Variable cost <br> per acre | Corn | Oats | Soybeans | Oats and <br> alfalfa | Diverted <br> land | Corn <br> silage |
| :--- | ---: | :---: | :---: | :---: | :---: | :---: |
| Fertilizer | $\$ 20.25$ | $\$ 6.00$ | $\$ 3.20$ | 0 | 0 | $\$ 20.55$ |
| Therapeutant | 2.80 | 0 | 0 | 0 | 0 | 2.80 |
| Herbacide | 3.82 | 0 | 4.70 | 0 | 0 | 3.82 |
| Seed | 4.34 | 4.40 | 3.10 | 0.54 | 1.64 | 4.34 |
| Op. costs (85 h.p. tractor) 3.53 | 2.06 | 2.86 | 3.07 | .81 | - |  |
| Op.costs (110 h.p. tractor) 3.04 | 1.65 | 2.40 | 2.51 | .68 | 11.32 |  |
| Total (85 h.p. tractor) | 34.74 | 12.46 | 13.86 | 9.61 | 2.45 | - |
| Total (110 h.p. tractor) | 34.25 | 12.05 | 13.40 | 9.05 | 2.32 | 42.83 |

[^9]| Table 7. Hogs: feed fed, cash expenses and net revenue per hog from |  |
| :--- | :--- |
| birth to slaughter (1968) |  |
| Item | Units |
| Weight at marketing | 220 lb |
| Price per cwt. | $\$ 17.00$ |
| Gross value | $\$ 37.40$ |
| Culled sow weight/hog sold | 5.34 lb |
| Sow value/hog sold | $\$ .80$ |
| Gross receipts | $\$ 38.20$ |
| Feed fed | 10.02 bu. |
| Corn | $\$ 8.95$ |

Annual cash expenses
Feed supplements $\quad \$ 8.95$
$\begin{array}{ll}\text { Power and machinery } & 1.18\end{array}$
Veterinary and med. $\quad 1.00$
Taxes (livestock and feed) and
interest on livestock

| Replacement boar | 1.02 |
| :--- | :---: |
| Total expenses | $\frac{12.71}{\$ 25.49}$ |
| Net revenue |  |

[^10]Table 8. Feeder swine: food fed, cash expenses and net revenue, per feeder pig for growing-finishing (1968) ${ }^{\text {a }}$

| Item | Unit |
| :---: | :---: |
| Weight at marketing | 220 1b |
| Weight when purchased | 40 lb |
| Price of weanlings | \$17.40 |
| Gross receipts at \$.17/1b | \$37.40 |
| Feed fed |  |
| Corn | 9.71 bu. |
| Supplements | \$4.75 |
| Annual cash expenses |  |
| Feed supplements | \$4.75 |
| Power and machinery | . 59 |
| Veterinary and med. | . 23 |
| Taxes (livestock and feed) and interest on livestock | . 23 |
| Price of weanling | 17.40 |
| Replacement boar | 1.02 |
| Total expenses | \$24.22 |
| Net revenue | \$13.18 |

[^11]Table 9. Weanling hogs: feed fed, cash expenses, and net revenue per hog (1968) ${ }^{\text {a }}$

| Item | Unit |
| :--- | :---: |
| Weight at sale (weaning) | 40 lb |
| Price per weanling | $\$ 16.60$ |
| Gross receipts | $\$ 16.60$ |
| Feed fed |  |
| Feed supplements ${ }^{\text {b }}$ | 5.20 |
| Corn | .322 bu |

Cash expenses
Feed supplements $\$ 5.20$
Power and machinery . 64
Veterinary and med. .87
Taxes (livestock and feed) and interest on livestock . 33

Replacement boar

Total expenses
8.96

Net revenue
$\$ 8.54$
${ }^{\text {a }}$ Source: Farm accounts and records and (4).
bincludes feed fed to sows and boars per piglet.

Table 10. Turkeys: Feed fed, cash expenses, and net revenue per turkey ${ }^{\text {a }}$

| Item | Unit (per 10 birds) |
| :---: | :---: |
| Weight at marketing | 2801 b |
| Price per lb | \$ . 20 |
| Gross value | 56.00 |
| Feed fed |  |
| Corn | 11.35 bushels |
| Supplements | \$14.87 |
| Annual cash expenses |  |
| Feed supplements ${ }^{\text {b }}$ | \$14.87 |
| Poults at $\$ .80 \mathrm{each}^{\text {c }}$ | 8.00 |
| Total expenses | \$22.87 |
| Net revenue | \$33.13 |

a Source: Farm accounts and records.
${ }^{\mathrm{b}}$ Feed supplements include the cost of medication added to the feed. $c^{c} \$ .10$ has been added to the cost of each poult to allow for death loss.
Table 1l. Buildings and equipment: capital requirements, useful life, and fixed costs ${ }^{\text {a }}$

Table 11. (Continued)

| Item | Repl. cost \$ | $\begin{gathered} \text { Life } \\ \text { (yrs) } \end{gathered}$ | Annual depr. | $\begin{gathered} \text { Av. repair } \\ \text { costs } \\ (1.5 \%) \\ \hline \end{gathered}$ | Taxes and insurance (1.3\%) | Total <br> fixed <br> costs |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Turkey Buildings and Equipment |  |  |  |  |  |  |
| 6000 bird brooding building Equipment for above | \$4,500 | 15 | 300.00 | 67.00 | 60.00 |  |
|  | 5,900 | 15 | 393.30 | 89.00 | 78.00 |  |
| Range shelters and feeders |  | 10 | 60.00 | 9.00 | 8.00 |  |
| Total Average value | 11,000 | $\begin{aligned} & 753.30 \quad 165.00 \\ & \text { Interest on average value } \end{aligned}$ |  |  | 146.00 |  |
|  | 5,500 |  |  |  | 146.00 | $\begin{array}{r} 1064.30 \\ 275.00 \end{array}$ |
|  |  |  |  |  |  | 1339.30 |
| Other |  |  |  |  |  |  |
| Houses (3) | 45,000 | 20 | 2250.00 | 675.50 | 600.00 |  |
| Two way radios (5) | 400 | 10 | 40.00 | 6.00 | 5.20 |  |
|  | 500 | 15 | 33.33 | 7.50 | 6.50 |  |
| Generator (auxilliary power)Welder | 653 | 10 | 65.30 | 9.79 | 8.49 |  |
|  | 335 | 10 | 33.50 | 5.03 | 4.35 |  |
| Well and water system | 1,500 | 20 | 75.00 | 22.50 | 19.50 |  |
| Machine shed and garage (2300 $\mathrm{ft}^{2}$ ) | 300 | 20 | 15.00 | 4.50 | 3.90 |  |
|  | 3,000 | 20 | 150.00 | 45.00 | 39.00 |  |
| Fences | 1,800 | 10 | 180.00 | 27.00 | 23.34 |  |
| Total | 53,488 | 2842.13 |  | 802.32 | 710.28 |  |
| Average value | 26,744 | Interest on average value $=$ |  |  |  | $\begin{array}{r}1337.20 \\ \hline\end{array}$ |
|  |  |  |  |  | 5691.93 |

Table 12. Approximate replacement cost of a twenty stall farrowing unit and related equipment, $1967^{\text {a }}$

## Item

Cost

I Building shell
A. Site preparation
$\$ 50.00$
B. Building shell ${ }^{\text {b }}$
3825.00
C. Utilities ${ }^{c}$
$1725.00-5600.00$

II Equipment
A. Steel farrowing stalls
$\$ 2400.00$
B. Electric floor heaters
600.00
C. Ventilation system
150.00
D. Self feeder for gestating sows
250.00
E. Heaters
200.00
$\underline{\underline{3600.00}}$
${ }^{\text {a }}$ Source: adapted from Trede (39).
bIncludes concrete foundations and floor, insulated walls and roof.
${ }^{{ }^{\text {I }}}$ Includes water supply, electrical outlets and sewage drains.

Table 13. Approximate replacement cost of a 500 head open front growingfinishing building for hogs, $1967^{\text {a }}$
Item
Cost

I Building Shell
A. Site preparation
\$ 120.00
B. Building shell ${ }^{\text {b }}$
4400.00
C. Utilities ${ }^{\text {C }}$
400.00
4920.00

II Equipment
A. Self feeders 800.00
B. Automatic heated waterers 400.00
C. Interior partitions 300.00
1500.00 6420.00
${ }^{\text {a }}$ Source: adapted from Trede (39).
${ }^{\mathrm{b}}$ Includes concrete foundations and floor, insulated walk and roof.
${ }^{\mathrm{C}}$ Includes water supply, electrical outlets and sewage drains.

Table 14. Approximate replacement costs of turkey facilities of 6,000 bird capacity (1967)a
Item

Cost
A. Brooding building ${ }^{\text {b }}$
\$ 4,500
B. Equipment for above ${ }^{c}$

5,900
C. Range shelters and feeders

$$
\$ 11,000.00
$$

$a_{\text {Replacement }}$ costs were developed in consultation with Mr. Wallace Ross, Department of Poultry Science, Iowa State University.
${ }^{b}$ Includes site preparation, concrete floor and foundation, insulated walls and roof.
c
Includes automatic feeders and waterers, gas heaters, thermostatically controlled ventilation, electric outlets and lights, and wire netting brooding frames.
Table 15. Cattle: input-output coefficients, variable costs, and net returns, using a self unloading wagon systema

| Cattle enterprise | 1 Steer calves |  | $\begin{aligned} & \quad 3 \\ & \text { Yearling } \\ & \text { steers } \end{aligned}$ | $\quad 4$ Yearling steers | $\quad 5$ Yearling steers | $\quad 6$ Yearling steers | 7 <br> Yearling <br> steers of | 8 Yearling steers of |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Unit: <br> Basic data: | 1 steer | 1 steer | 1 steer | 1 steer | 1 steer | 1 steer | 2 steers | 2 steers |
| Purch. date | Nov | Nov | Oct | Oct | April | April | Oct.Apr. | Oct.Apr. |
| Markt. date | Aug | Aug | Apr | Apr | Sept | Sept | Apr. Sept. | Apr. Sept |
| Days fed | 270 | 270 | 190 | 190 | 145 | 145 | 335 | 335 |
| Init. weight(lb) | 450 | 450 | 600 | 600 | 700 | 700 | 1300 | 1300 |
| Mkt weight (1b) | 1050 | 1050 | 1050 | 1050 | 1050 | 1050 | 2100 | 2100 |
| Net gain (1b) | 600 | 600 | 450 | 450 | 350 | 350 | 800 | 800 |
| Gain/day | 2.22 | 2.22 | 2.37 | 2.37 | 2.42 | 2.42 |  |  |
| Death loss (\%) | 1.10 | 1.10 | . 75 | . 75 | . 75 | . 75 | . 75 | . 75 |
| Meat sold (lb) | 1020 | 1020 | 1020 | 1020 | 1020 | 1020 | 2040 | 2040 |
| Feed fed: |  |  |  |  |  |  |  |  |
| Corn (bu) | 44.4 | 43.7 | 47.6 | 44.5 | 36.25 | 37.03 | 83.85 | 81.53 |
| Suppl. (lb) | 194.4 | 37.8 | 89.3 | 43.7 | 68.15 | 33.35 | 157.45 | 77.05 |
| Haylage (tons) | 0 | . 742 | 0 | . 294 | 0 | . 224 | 0 | . 518 |
| Silage (tons) | 2.632 | 1.620 | 1.710 | 1.197 | 1.305 | . 913 | 3.015 | 2.110 |
| Labor 1 | 1.82 | 1.82 | 1.78 | 1.78 | 0 | 0 | 1.78 | 1.78 |
| Labor 2 | 1.20 | 1.20 | . 98 | . 98 | . 47 | . 47 | 1.45 | 1.45 |
| Labor 3 | . 95 | . 95 | 0 | 0 | 1.36 | 1.36 | 1.36 | 1.36 |
| Labor 4 | . 35 | . 35 | 0 | 0 | 1.36 | 1.36 | 1.36 | 1.36 |
| Labor 5 | . 12 | . 12 | . 14 | . 14 | . 43 | . 43 | . 57 | . 51 |

a Source: (27) and private communication with G. D. Harter.
Table 15. (Continued)

| Cattle enterprise |  |  | 3 <br> Yearling <br> steers | 4 <br> Yearling steers | $\begin{aligned} & \quad 5 \\ & \text { Yearling } \\ & \text { steers } \end{aligned}$ | $\begin{aligned} & \quad 6 \\ & \text { Yearling } \\ & \text { steers } \end{aligned}$ | $\begin{aligned} & 7 \\ & \text { Yearling } \\ & \text { steers of } \end{aligned}$ | $\begin{gathered} 8 \\ \text { Yearling } \\ \text { steers of } \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Variable costs: |  |  |  |  |  |  |  |  |
| Suppl. (5¢/1b) | 9.72 | 1.89 | 4.46 | 2.19 | 3.41 | 1.66 | 7.87 | 3.85 |
| Power and machinery | 4.63 | 4.63 | 1.51 | 1.51 | 1.08 | 1.08 | 2.59 | 2.59 |
| Taxes on LS | . 97 | . 97 | . 97 | . 97 | . 88 | . 88 | 1.85 | 1.85 |
| Vet and med. | 4.50 | 4.50 | 1.20 | 1.20 | . 85 | . 85 | 2.05 | 2.05 |
| Transport | 4.85 | 4.85 | 5.00 | 5.00 | 5.00 | 5.00 | 10.00 | 10.00 |
| Feeder stock | 129.62 | 129.62 | 160.80 | 160.80 | 174.19 | 174.19 | 334.99 | 334.99 |
| Interest on LS | 6.28 | 6.28 | 6.42 | 6.42 | 6.33 | 6.33 | 12.75 | 12.75 |
| ```Cost of feedlot/ steer/yr:``` |  |  |  |  |  |  |  |  |
| 0-350 head | 6.44 | 6.44 | 6.44 | 6.44 | 6.44 | 6.44 | 3.22 | 3.22 |
| 351-500 head | 5.98 | 5.98 | 5.98 | 5.98 | 5.98 | 5.98 | 2.99 | 2.99 |
| 500-750 head | 5.22 | 5.22 | 5.22 | 5.22 | 5.22 | 5.22 | 2.61 | 2.61 |
| Total variable costs |  |  |  |  |  |  |  |  |
| 0-350 head capac. | 167.01 | 159.18 | 186.80 | 184.53 | 198.18 | 196.43 | 375.32 | 371.30 |
| 351-500 " " | 166.55 | 158.72 | 186.34 | 184.07 | 197.72 | 195.97 | 375.09 | 371.07 |
| 500-750 " " | 165.79 | 157.96 | 185.58 | 183.31 | 196.96 | 195.21 | 374.71 | 370.69 |
| Gross receipts | 278.50 | 278.50 | 274.60 | 274.60 | 271.80 | 271.80 | 546.40 | 546.40 |
| Net revenue |  |  |  |  |  |  |  |  |
| 0-350 head unit | 111.49 | 119.32 | 87.80 | 90.07 | 73.62 | 75.37 | 171.08 | 175.10 |
| 351-500 " " | 111.95 | 119.78 | 88.26 | 90.53 | 74.09 | 75.83 | 171.31 | 175.33 |
| 500-750 " " | 112.71 | 120.54 | 89.02 | 91.29 | 74.84 | 76.59 | 171.69 | 175.71 |

Table 16. Cattle: input-output coefficients, variable costs, and net returns using an auger feeding systema

| Cattle enterprise | $\begin{gathered} \text { Calf } \\ 1 \end{gathered}$ | $\begin{gathered} \text { Calf } \\ 2 \end{gathered}$ | $\begin{gathered} \text { Yrling } \\ 3 \end{gathered}$ | $\underset{4}{\text { Yrling }}$ | Steer 5 | Steer <br> 6 | $\begin{gathered} \text { Yrling } \\ 8 \end{gathered}$ | $\underset{9}{\text { Yrling }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Basic data: |  |  |  |  |  |  |  |  |
| Feed fed <br> Variable costs excluding | As for the respective columns in Table 15 |  |  |  |  |  |  |  |
| Labor 1 | 1.26 | 1.26 | 1.44 | 1.44 | 0 | 0 | 1.44 | 1.44 |
| 2 | . 95 | . 95 | . 79 | . 79 | . 33 | . 33 | 1.12 | 1.12 |
| 3 | . 72 | . 72 | 0 | 0 | 1.17 | 1.17 | 1.17 | 1.17 |
| 4 | . 26 | .26 | 0 | 0 | 1.17 | 1.17 | 1.17 | 1.17 |
| 5 | . 08 | . 08 | . 11 | .11 | . 30 | . 30 | . 41 | . 41 |
| Cost of feedlot/steer/yr |  |  |  |  |  |  |  |  |
| $0-350$ head | 7.07 | 7.07 | 7.07 | 7.07 | 7.07 | 7.07 | 3.53 | 3.53 |
| 351-500" | 6.49 | 6.49 | 6.49 | 6.49 | 6.49 | 6.49 | 3.24 | 3.24 |
| Total variable costs |  |  |  |  |  |  |  |  |
| 0-350 hed capacity | 167.64 | 159.81 | 187.43 | 185.16 | 198.81 | 197.06 | 375.63 | 371.61 |
| 351 - 500 " | 167.06 | 159.23 | 186.85 | 184.58 | 198.23 | 196.48 | 375.34 | 371.32 |
| Gross receipts | 278.50 | 278.50 | 274.60 | 274.60 | 271.80 | 271.80 | 546.40 | 546.40 |
| Net revenue |  |  |  |  |  |  |  |  |
| $0-350$ head unit | 110.86 | 118.69 | 87.17 | 89.44 | 72.99 | 74.74 | 170.77 | 174.79 |
| 351 - 500 head unit | 111.44 | 119.27 | 87.75 | 90.02 | 73.57 | 75.32 | 171.06 | 175.08 |

Table 17. Annual fixed costs of various sized farms used in the study ${ }^{\text {a }}$

| Item | Farm size in acres |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | 720 | 1040 | 1360 | 1680 | 2000 |
| Property taxes | 4,932.50 | 7,966.00 | 10,999.47 | 13,845.53 | 17,071.38 |
| Int. on land ${ }^{\text {b }}$ | 21,840.00 | 35,280.00 | 48,720.00 | 61,320.00 | 75,600.00 |
| Rent | 4,230.00 | 4,230.00 | 4,230.00 | 4,230.00 | 4,230.00 |
| Machinery | 6,264.00 | 9,764.00 | 9,764.00 | 12,832.00 | 12,832.00 |
| ```Corn cribs, grinder-mixer etc.``` | 3,302.50 | 3,302.50 | 4,649.81 | 4,649.81 | 4,649.81 |
| Hog bldgs and equip. | 1,844.40 | 1,844.40 | 1,844.40 | 1,844.40 | 1,844.40 |
| Turkey " | 1,339.30 | 1,339.30 | 1,339.30 | 1,339.30 | 1,339.30 |
| Houses, sheds and misc. | 5,691.93 | 5,691.93 | 5,920.40 | 6,854.14 | 6,856.14 |
| Tiles | 585.00 | 944.77 | 1,304.55 | 1,638.00 | 2,024.10 |
| Labor(3 units) | 37,300.00 | 37,300.00 | 37,300.00 | 37,300.00 | 37,300.00 |
| Labor (4 units) | 45,300.00 | 45,300.00 | 45,300.00 | 45,300.00 | 45,300.00 |
| Labor (5 units) | - | - | 53,300.00 | 53,300.00 | 53,300.00 |
| Total(3 lab. units) | 87,329.63 | 107,662.90 | 126,071.93 | 145,853.18 | 163,745.13 |
| Total (4 ") | 95,329.63 | 115,662.90 | 134,071.93 | 153,853.18 | 171,745.13 |
| Total (5 ") | - | - | 142,071.93 | 161,853.18 | 179,745.13 |

$a_{\text {Farm records, Tables } 9,15 .}$
${ }^{\mathrm{b}}$ Calculated as: Total acreage less 200 rented acres, at $6 \%$ per annum.

XI . APPENDIX B
Table 18. Optimum plans for Model 1 (720 acres)

| Activity Name | BJl | BJ5 | BJ7 | BJ2 | BJ6 | BJ8 | Units |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Gross returns | 116,882 | 114,211 | 111,792 | 125,678 | 123,009 | 120,544 | \$ |
| Net profit | 29,554 | 26,883 | 24,485 | 30,350 | 27,681 | 25,237 | \$ |
| Labor units | 3 | 3 | 3 | 4 | 4 | 4 | men |
| Corn | 614 | 420 | 280 | 614 | 420 | 280 | acres |
| Turkey land | 66 | 66 | 66 | 66 | 66 | 66 | " |
| Soybeans | 0 | 194 | 264 | 0 | 194 | 264 | " |
| Diverted land | 0 | 0 | 70 | 0 | 0 | 70 | " |
| Buy corn 1 | 210 | 6,228 | 4,708 | 1,954 | 7,803 | 7,372 | bushels |
| Buy corn 2 | 2,496 | 7,955 | 0 | 2,600 | 8,351 | 0 |  |
| Buy corn 4 | 2,485 | 9,238 | 18,786 | 4,215 | 10,940 | 20,445 | " |
| Sell corn 3 | 58,520 | 52,500 | 35,000 | 58,375 | 52,500 | 35,000 | " |
| Sell oats 3 | 3,102 | 0 | 0 | 3,102 | 0 | 0 | " |
| Sell oats 4 | 0 | 3,102 | 3,102 | 0 | 3,102 | 3,102 | " |
| Sell soybeans 3 | 0 | 3,102 | 3,102 | 0 | 3,102 | 3,102 | " |
| Sell soybeans 4 | 0 | 4,658 | 7,458 | 0 | 4,658 | 7,458 | " |
| Sell hay | 50.8 | 50.8 | 50.8 | 50.8 | 50.8 | 50.8 | tons |
| Hogs 1 | 0 | 0 | 0 | 0 | 340 | 418 | head |
| Weanlings 1 | 355 | 345 | 500 | 500 | 500 | 500 | " |
| Weanlings 2 | 500 | 500 | 500 | 500 | 500 | 500 | " |
| Weanlings 3 | 66 | 55 | 0 | 280 | 290 | 290 | " |
| Weanlings 4 | 138 | 160 | 216 | 154 | 160 | 82 | " |
| Turkeys | 20,000 | 20,000 | 20,000 | 20,000 | 20,000 | 20,000 | " |
| C P. transfer 1 | 50,925 | 53,643 | 40,590 | 52,919 | 55,949 | 42,549 | \$ |
| Cap. transfer 2 | 0 | 0 | 0 | 0 | 0 | 0 |  |
| Cap. transfer 3 | 78,780 | 78,207 | 37,946 | 78,554 | 78,270 | 37,728 | " |
| Cap. transfer 4 | 99,799 | 106,270 | 63,835 | 93,889 | 100,609 | 56,554 | " |
| Labor 1 | 4.8 | 3.3 | 2.3 | 3.5 | 3.5 | 3.5 | hours/day |
| Labor 2 | 8.0 | 8.0 | 8.0 | 8.0 | 8.0 | 8.0 | " |
| Labor 3 | 11.5 | 11.5 | 11.4 | 10.3 | 8.9 | 10.0 | " |
| Labor 4 | 8.5 | 8.5 | 8.5 | 8.5 | 8.5 | 8.8 | " |
| Labor 5 | 8.5 | 7.6 | 7.4 | 7.6 | 7.1 | 6.7 | " |

Table 19. Optimum plans for model 1 when 620 acres of land are rented out at $\$ 50$ per acre

| Activity Name | BJIR | BJ2R | Units |
| :---: | :---: | :---: | :---: |
| Labor units | 3 | 4 | Men |
| Gross returns | 102,294 | 111,523 | \$ |
| Net profit | 23,494 | 24,723 | \$ |
| Rented Iand | 620 | 620 | acres |
| Turkey pasture | 80 | 80 | " |
| Buy corn 4 | 33,871 | 39,925 | bushels |
| Sell oats 3 | 3,760 | 3,760 | " |
| Sell hay | 61.6 | 61.6 | tons |
| Hogs 1 | 327 | 420 | head |
| Hog expansion 1 | 0 | 281 | head |
| Hog expansion 3 | 233 | 448 | " |
| Weanlings 1 | 500 | 500 | " |
| Weanlings 2 | 500 | 500 | " |
| Turkeys | 20,000 | 20,000 | " |
| Turkey expansion | 4,240 | 4,240 | " |
| Capital transfer 1 | 35,878 | 39,492 | \$ |
| Capital transfer 3 | 24,638 | 29,056 | " |
| Capital transfer 4 | 25,390 | 18,835 | " |
| Labor 1 | 3.8 | 4.4 | hours/day |
| Labor 2 | 8.0 | 8.0 | " |
| Labor 3 | 9.6 | 9.0 | " |
| Labor 4 | 8.5 | 8.5 | " |
| Labor 5 | 6 | 5.9 | " |

Table 20. Optimum plans for model 2 (1040 acres)

| Activity | BO1 | B07 | B14 | B02 | B08 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Labor units | 3 | 3 | 3 | 4 | 4 |
| Gross return | 152,766 | 150,588 | 141,727 | 180,938 | 179,150 |
| Net profit | 44,848 | 42,493 | 34,143 | 64,897 | 62,845 |
| Corn | 892 | 600 | 227 | 840 | 600 |
| Turkey pasture | 90 | 92 | 89 | 142 | 142 |
| Soybeans | 0 | 290 | 402 | 0 | 240 |
| Diverted land | 0 | 0 | 264 | 0 | 0 |
| Buy corn 1 | 318 | 656 | 0 | 799 | 1,032 |
| Buy corn 2 | 3,397 | 3,323 | 0 | 5,042 | 5,001 |
| Buy corn 4 | 12,520 | 13,120 | 34,706 | 20,567 | 20,833 |
| Sell corn 3 | 95,944 | 59,152 | 28,375 | 80,342 | 50,296 |
| Sell oats 2 | 4,227 | 4,311 | 4,204 | 6,669 | 6,669 |
| Sell beans 3 | 0 | 11,609 | 16,062 | 0 | 9,604 |
| Sell haylage | 94.7 | 97 | 98.4 | 156 | 156 |
| Feeders 1 | 0 | 78 | 205 | 165 | 213 |
| Feeders 4 | 0 | 0 | 201 | 0 | 67 |
| Turkeys | 13,000 | 13,000 | 13,000 | 13,000 | 13,000 |
| Turkey expansion | 14,250 | 14,790 | 14,100 | 30,000 | 30,000 |
| Weanlings 1 | 0 | 0 | 0 | 0 | 0 |
| Weanlings 2 | 172 | 0 | 0 | 143 | 83 |
| Weanlings exp. 2 | 0 | 0 | 0 | 0 | 0 |
| Cap. transfer 1 | 64,715 | 62,306 | 45,625 | 84,612 | 81,260 |
| Cap. transfer 3 | 66,568 | 56,769 | 54,078 | 139,863 | 44,258 |
| Cap. transfer 4 | 59,579 | 83,751 | 62,074 | 107,056 | 101,125 |
| Labor 1 | 1.9 | 1.3 | 1.1 | 1.4 | 1.3 |
| Labor 2 | 8.0 | 8.0 | 8.0 | 8.0 | 8.0 |
| Labor 3 | 11.5 | 11.5 | 11.5 | 11.5 | 11.5 |
| Labor 4 | 8.5 | 8.5 | 8.5 | 8.5 | 8.5 |
| Labor 5 | 6.8 | 6.0 | 5.0 | 5.9 | 4.4 |
| Buy grain bins | 41,398 | 12,200 | 0 | 35,012 | 7,935 |


| B15 | B03 | B09 | B17 | Units |
| :---: | :---: | :---: | :---: | :---: |
| 4 | 5 | 5 | 5 | Men |
| 170,442 | 201,444 | 199,889 | 194,045 | \$ |
| 54,876 | 77,379 | 75,557 | 70,406 | \$ |
| 227 | 840 | 600 | 294 | Acres |
| 139 | 142 | 142 | 142 | " |
| 352 | 0 | 240 | 349 | " |
| 264 | 0 | 0 | 197 | " |
| 4,290 | 1,204 | 819 | 7,389 | Bushels |
|  | 8,283 | 8,299 | 5,636 |  |
| 49,737 | 20,308 | 20,364 | 39,387 | " |
| 28,375 | 77,493 | 47,559 | 36,533 | " |
| 6,548 | 6,669 | 6,669 | 6,669 | " |
| 14,067 | 0 | 9,575 | 13,960 | " |
| 153 | 156 | 156 | 156 | Tons |
| 350 | 0 | 0 | 0 | Head |
| 280 | 0 | 0 | 64 | " |
| 13,000 | 13,000 | 13,000 | 13,000 | " |
| 29,220 | 30,000 | 30,000 | 30,000 | " |
| 0 | 0 | 0 | 500 | " |
| 0 | 500 | 500 | 500 | " |
| 0 | 1,008 | 1,006 | 1,050 | " |
| 60,222 | 89,137 | 88,211 | 56,004 | \$ |
| 50,800 | 152,740 | 134,228 | 48,710 | \$ |
| 77,588 | 127,419 | 121,680 | 84,203 | \$ |
| 0.9 | 6.0 | 6.0 | 6.0 | hours/day |
| 8.0 | 8.0 | 8.0 | 8.0 | " |
| 11.5 | 10.1 | 10.1 | 10.0 | " |
| 8.5 | 8.5 | 8.5 | 8.5 | " |
| 4.6 | 10.2 | 10.2 | 10.2 | " |
| 0 | 32,448 | 7,442 | 0 | bushels |

Table 21. Optimum plans for Model 3 (1360 acres)

| Activity | BO1 | B10 | B14 | B02 | B08 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Labor units | 3 | 3 | 3 | 4 | 4 |
| Gross return | 164,546 | 166,113 | 157,759 | 200,300 | 197,612 |
| Net profit | 38,474 | 40,042 | 31,755 | 66,228 | 63,540 |
| Corn grain | 439 | 592 | 321 | 1,163 | 799 |
| Corn silage | 3 | 2 | 0 | 0.6 | 0.7 |
| Turkey pasture | 67 | 70 | 71 | 121 | 124 |
| Soybeans | 775 | 572 | 571 | 0 | 361 |
| Diverted land | 0 | 49 | 322 | 0 | 0 |
| Buy corn 1 | 1,284 | 797 | 611 | 246 | 826 |
| Buy corn 2 | 6,093 | 6,109 | 12,807 | 10,234 | 10,299 |
| Buy corn 3 | 9,930 | 19,067 | 11,209 | 16,761 | 17,756 |
| Sell corn 3 | 46,520 | 65,246 | 37,456 | 130,282 | 84,400 |
| Sell oats 1 | 3,160 | 3,298 | 3,346 | 5,693 | 5,840 |
| Sell beans 3 | 30,997 | 22,867 | 22,832 | 0 | 14,428 |
| Sell haylage | 57 | 66.6 | 78.3 | 130 | 133 |
| Feeders 1 | 0 | 0 | 126 | 0 | 113 |
| Feeders 4 | 0 | 0 | 170 | 0 | 0 |
| Weanlings 2 | 0 | 0 | 0 | 304 | 0 |
| Weanling exp. 2 | 0 | 0 | 0 | 0 | 0 |
| Turkeys | 13,000 | 13,000 | 13,000 | 13,000 | 13,000 |
| Turkey expansion | 7,380 | 8,264 | 8,573 | 23,700 | 24,654 |
| Yearlings 42A | 58 | 36 | 0 | 11 | 13 |
| Steers 42B | 0 | 0 | 0 | 0 | 0 |
| Calves 22A | 0 | 0 | 0 | 0 | 0 |
| Cap. transfer 1 | 57,283 | 64,867 | 102,742 | 98,554 | 95,630 |
| Cap. transfer 3 | 95,468 | 97,899 | 120,356 | 104,888 | 96,053 |
| Cap, transfer | 89,721 | 97,097 | 129,429 | 133,419 | 125,910 |
| Labor 1 | 1.6 | 1.8 | 1.2 | 2.1 | 1.3 |
| Labor 2 | 8.0 | 8.0 | 8.0 | 8.0 | 8.0 |
| Labor 3 | 11.5 | 11.5 | 11.5 | 11.5 | 11.5 |
| Labor 4 | 8.5 | 8.5 | 8.5 | 8.5 | 8.5 |
| Labor 5 | 6.3 | 6.2 | 5.4 | 6.9 | 6.0 |
| Buy grain bins | 15,910 | 26,872 | 0 | 81,093 | 44,338 |


| B15 | B03 | B09 | B17 | Units |
| :---: | :---: | :---: | :---: | :---: |
| 4 | 5 | 5 | 5 | Men |
| 185,902 | 223,760 | 221,388 | 213,136 | \$ |
| 51,930 | 81,688 | 79,316 | 71,064 | " |
| 321 | 1,139 | 799 | 386 | acres |
| 0 | 4 | 0.6 | 0 | " |
| 121 | 142 | 142 | 142 | " |
| 521 | 0 | 343 | 499 | " |
| 322 | 0 | 0 | 257 | bushels |
| 1,309 | 901 | 120 | 351 | " |
| 18,885 | 13,448 | 13,131 | 17,542 | " |
| 19,138 | 19,698 | 19,509 | 42,090 | " |
| 32,841 | 124,085 | 82,161 | 25,447 | " |
| 5,690 | 6,669 | 6,669 | 6,669 | " |
| 20,837 | 0 | 13,723 | 19,948 | tons |
| 133 | 116 | 151 | 78 | head |
| 270 | 0 | 0 | 72 | " |
| 250 | 0 | 0 | 0 | " |
| 0 | 500 | 500 | 500 | " |
| 0 | 1,004 | 1,007 | 61 | " |
| 13,000 | 13,000 | 13,000 | 13,000 | " |
| 23,688 | 30,000 | 30,000 | 30,000 | " |
| 0 | 0 | 0 | 0 | " |
| 0 | 0 | 0 | 348 | " |
| 0 | 53 | 7 | 0 | " |
| 143,914 | 183,881 | 92,783 | 225,402 | \$ |
| 132,625 | 186,905 | 85,382 | 124,506 | " |
| 167,880 | 227,303 | 127,552 | 255,014 | " |
| 1.0 | 4.9 | 5.4 | 1.9 | hours/day |
| 8.0 | 8.0 | 8.0 | 8.0 | " |
| 11.5 | 10.1 | 10.1 | 11.5 | " |
| 8.5 | 8.5 | 8.5 | 8.5 | " |
| 5.0 | 7.9 | 7.9 | 5.1 | " |
| 0 | 79,000 | 43,652 | 0 | bushels |

Table 22. Optimum plans for Model 4 (1680 acres)

| Activity | B01 | B10 | B1 4 | B02 |
| :---: | :---: | :---: | :---: | :---: |
| Labor units | 3 | 3 | 3 | 4 |
| Gross return | 174,024 | 180,340 | 176,586 | 213,830 |
| Net profit | 28,168 | 34,484 | 28,789 | 59,974 |
| Corn grain | 0 | 291 | 400 | 819 |
| Corn silage | 9.6 | 1 | 0 | 4 |
| Turkey pasture | 33 | 51 | 52 | 99 |
| Soybeans | 1,557 | 1,096 | 748 | 678 |
| Diverted land | 0 | 160 | 400 | 0 |
| Buy corn 1 | 7,373 | 403 | 248 | 1,455 |
| Buy corn 2 | 4,836 | 4,393 | 4,253 | 8,755 |
| Buy corn 4 | 6,524 | 7,278 | 8,125 | 14,355 |
| Sell corn 3 | 0 | 30,006 | 42,770 | 90,005 |
| Sell oats 1 | 1,537 | 2,416 | 2,442 | 4,643 |
| Sell beans 3 | 62,282 | 43,843 | 29,921 | 27,140 |
| Sell haylage | 0 | 51 | 57 | 89 |
| Buy haylage | 13.5 | 0 | 0 | 0 |
| Feeders 4 | 0 | 0 | 153 | 0 |
| Feeders 1 | 0 | 0 | 61 | 0 |
| Weanlings 2 | 0 | 0 | 0 | 0 |
| Weanling exp. 2 | 0 | 0 | 0 | 0 |
| Turkeys | 9,910 | 13,000 | 13,000 | 13,000 |
| Turkey expansion | 0 | 2,580 | 2,745 | 10,938 |
| Yearlings 42A | 168 | 18 | 0 | 66 |
| Steers 42B | 0 | 0 | 0 | 0 |
| Cap. transfer 1 | 19,419 | 63,144 | 64,078 | 81,833 |
| Cap. transfer 3 | 113,210 | 111,645 | 105,204 | 120,717 |
| Cap. transfer 4 | 64,577 | 99,404 | 98,554 | 122,990 |
| Labor 1 | 2.9 | 1.6 | 1.3 | 1.7 |
| Labor 2 | 8.0 | 8.0 | 8.0 | 8.0 |
| Labor 3 | 11.0 | 11.5 | 11.5 | 11.5 |
| Labor 4 | 8.5 | 8.5 | 8.5 | 8.5 |
| Labor 5 | 5.9 | 6.0 | 5.8 | 6.3 |
| Buy grain bins | 0 | 10,267 | 9,922 | 59,477 |


| B11. | B15 | BO3 | B16 | B17 | Unit |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | 4 | 5 | 5 | 5 | men |
| 213,643 | 202,759 | 247,106 | 242,240 | 232,950 | \$ |
| 59,787 | 48,996 | 85,250 | 80,384 | 71,188 | " |
| 796 | 400 | 1,452 | 800 | 480 | acres |
| 4 | 0 | 5 | 0 | 0 | " |
| 99 | 102 | 142 | 142 | 142 | " |
| 701 | 698 | 0 | 658 | 658 | " |
| 0 | 400 | 0 | 0 | 320 | " |
| 1,458 | 945 | 1,177 | 17 | 882 | bushels |
| 8,748 | 8,336 | 12,772 | 12,595 | 12,494 | " |
| 14,365 | 16,053 | 19,764 | 19,759 | 21,813 | " |
| 87,206 | 36,160 | 163,127 | 81,486 | 40,163 | " |
| 4,643 | 4,786 | 6,669 | 6,669 | 6,669 | " |
| 28,038 | 27,926 | 0 | 0 | 26,316 | " |
| 90 | 112 | 104 | 147 | 145 | tons |
| 0 | 0 | 0 | 0 | 0 | " |
| 0 | 223 | 0 | 0 | 232 | " |
| 0 | 182 | 0 | 3 | 182 | head |
| 0 | 0 | 433 | 500 | 500 | " |
| 0 | 0 | 0 | 306 | 0 | " |
| 13,000 | 13,000 | 13,000 | 13,000 | 13,000 | " |
| 16,938 | 17,860 | 30,000 | 30,999 | 30,000 | " |
| 65 | 0 | 0 | 0 | 0 | " |
| 0 | 0 | 0 | 40 | 50 | " |
| 81,660 | 82,899 | 209,556 | 116,442 | 107,129 | \$ |
| 120,165 | 95,011 | 228,830 | 108,621 | 87,034 | " |
| 122,603 | 114,543 | 262,550 | 155,779 | 140,270 | " |
| 1.7 | 1.2 | 2.5 | 2.8 | 2.0 | hours/day |
| 8.0 | 8.0 | 8.0 | 8.0 | 8.0 | " |
| 11.5 | 11.5 | 11.2 | 11.5 | 11.5 | " |
| 8.5 | 8.5 | 8.5 | 8.5 | 8.5 | " |
| 6.3 | 5.3 | 7.0 | 6.6 | 5.6 | " |
| 57,575 | 7,926 | 118,225 | 56,317 | 16,316 | bushels |

Table 23. Optimum plans for Model 5 (2000 acres)

| Activity | B10 | B12 | B14 | B02 |
| :--- | :---: | :---: | :---: | :---: |


| Labor units | 3 | 3 | 3 | 4 |
| :---: | :---: | :---: | :---: | :---: |
| Gross return | 190,436 | 193,998 | 191,239 | 224,660 |
| Net profit | 26,688 | 30,250 | 27,532 | 52,918 |
| Corn grain | 0 | 465 | 480 | 161 |
| Corn silage | 8 | 0 | 0 | 6 |
| Turkey pasture | 16 | 33 | 32 | 73 |
| Soybeans | 1,704 | 1,038 | 928 | 1,680 |
| Diverted land | 192 | 384 | 480 | 0 |
| Buy corn 1 | 3,036 | 0 | 0 | 2,178 |
| Buy corn 2 | 4,665 | 2,720 | 2,654 | 6,974 |
| Buy corn 4 | 3,827 | 4,563 | 4,945 | 11,206 |
| Sell corn 3 | 0 | 53,592 | 55,459 | 11,007 |
| Sell oats 1 | 744 | 1,562 | 1,524 | 3,430 |
| Sell beans 3 | 68,153 | 41,518 | 37,103 | 67,204 |
| Sell haylage | 0 | 36 | 36 | 51 |
| Buy haylage | 23 | 0 | 0 | 0 |
| Feeders 1 | 0 | 0 | 0 | 0 |
| Feeders 4 | 0 | 0 | 102 | 0 |
| Turkeys | 4,795 | 10,070 | 9,825 | 13,000 |
| Turkey expansion | 0 | 0 | 0 | 9,116 |
| Yearlings 42A | 137 | 0 | 0 | 0 |
| Cap. transfer 1 | 26,039 | 66,795 | 92,072 | 62,035 |
| Cap. transfer 3 | 128,688 | 133,485 | 156,976 | 127,417 |
| Cap. transfer 4 | 71,327 | 108,613 | 133,762 | 107,214 |
| Labor 1 | 2.7 | 1.6 | 1.5 | 2.0 |
| Labor 2 | 8.0 | 8.0 | 8.0 | 8.0 |
| Labor 3 | 10.5 | 11.0 | 11.1 | 11.5 |
| Labor 4 | 8.5 | 8.5 | 8.5 | 8.5 |
| Labor 5 | 6.0 | 6.4 | 6.2 | 5.8 |
| Buy grain bins | 128 | 29,619 | 27,103 | 17,320 |


| B11 | B15 | B03 | B16 | B17 | Unit |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 4 | 4 | 5 | 5 | 5 | Men |
| 230,819 | 219,735 | 263,283 | 261,355 | 251,697 | \$ |
| 59,071 | 48,073 | 83,535 | 81,607 | 72,036 | " |
| 760 | 480 | 1,188 | 956 | 576 | Acres |
| 1 | 0 | 4 | 4 | 0 | " |
| 84 | 82 | 130 | 130 | 133 | " |
| 882 | 878 | 598 | 830 | 827 | " |
| 192 | 480 | 0 | 0 | 384 | " |
| 268 | 576 | 1,638 | 1,667 | 1,090 | bushels |
| 7,038 | 6,736 | 11,388 | 11,316 | 10,921 | " |
| 11,743 | 12,921 | 18,731 | 18,835 | 20,461 | " |
| 84,507 | 48,680 | 132,256 | 103,303 | 54,291 | " |
| 3,971 | 3,868 | 6,108 | 6,108 | 6,271 | - |
| 35,294 | 35,108 | 23,910 | 33,191 | 33,063 | " |
| 89 | 90 | 121 | 123 | 147 | tons |
| 0 | 0 | 0 | 0 | 0 | " |
| 0 | 119 | 0 | 39 | 225 | head |
| 0 | 216 | 0 | 0 | 217 | " |
| 13,000 | 13,000 | 13,000 | 13,000 | 13,000 | " |
| 12,600 | 11,940 | 26,378 | 26,383 | 27,435 | " |
| 12 | 0 | 74 | 67 | 0 | " |
| 91,803 | 131,127 | 105,531 | 103,743 | 178,083 | \$ |
| 136,961 | 166,417 | 144,442 | 150,925 | 186,611 | " |
| 136,966 | 170,350 | 154,927 | 138,733 | 216,130 | " |
| 1.5 | 1.3 | 1.7 | 1.6 | 1.2 | hrs/day |
| 8.0 | 8.0 | 8.0 | 8.0 | 8.0 | " |
| 11.5 | 11.5 | 11.5 | 11.5 | 11.5 | " |
| 8.5 | 8.5 | 8.5 | 8.5 | 8.5 | " |
| 6.3 | 5.6 | 6.4 | 6.2 | 5.4 |  |
| 60,347 | 25,108 | 102,386 | 82,716 | 35,063 | bushels |

X. APPENDIX C

TALLE 24 . UCMFUTER PRLATOUT LFFMUEL 5.
RCLIS
N RETURNS
L LANLA
L LANDB
L LANUC
1 RHSA
1 KHSE
$L$ intise
1 ritisu
L TURKLANL
L (UKNPRLU
L CUisins IL
L CATGFA
L BEANS
L HAYL
L LABCk 1
L LABURC
L LABLK3
L LABUR4
L LABORS
L CAPSPLYI

1. CAPSPLYZ

L CAPSPLY3
1 LAPSPLV4
E FCUSTSI
E FCCSTSE
E FCOSTS 3
$t$ FClisis4
E PLKICLI
E PERIGNZ
E PE\&ICU3
E PEKIOD4
L PERILDIA
E PLR1しट2A
$E$ PERIGD3A
E PERIOD4A
E PERICD1L
E PERIOU22
E PERICU33
L PEKICU44
L G $\quad$ RMAXI
1 GSTKMAXZ
L uSTRMAX3
L GSIRMAX4
L. TUKKMAXI
L. JJRKMAXE

1. FARCMAXL

L t ARLGMAX
L. IArLMAX3
table 24．（clatinlid）．
L farcmax4
L fieumaxi
L feELMAXZ
L FEEDNAX3
L FEEDMAX4

## COLUMNS

CLRNG
CuRNG
CCRNG
CORNG
CORNG
CCRNG
CORNG
cerns
CURINS
ceras
cerns
cerns
CLRNS
pastuke
pasture
pasture
pASTURE
PASTURE
PASTLKE
PASTURE
PASTLRE
LATS
CATS
RETLKAS

| -34.740 | LANDA |
| ---: | :--- |
| .280 |  |
| .430 | LABUR3 |
| .790 | LABCR5 |
| .240 | CAPSPLY2 |
| 4.110 | CAPSPLY4 |
| -125.00 C | CLRNPRUD |
| -42.770 | LANUA |
| -21.00 C | LABCR1 |
| .430 | LABUR3 |
| 3.010 | LABLR5 |
| .270 | CAPSPLY |
| 8.80 C | CAPSPLY4 |
| $-9.05 C$ | LANDC |

1.000

LAEOR 1
LABCK2
LABOR 4
CAPSPLYI
CAPSPLY3
PER IOD 44
RETURNS
CURNSIL LABCLR2
LABCR4
CAP SPLYI
CAPSPLY3 RETURNS TURKLAIND HAYL
LAEURZ
LABOR4
CAPSPLYI
CAPSPLY3 pericuza RETUKNS Cat GRiv
CATS
LABCRZ
EATS
CATS
UATS
LATS
scybas
SLYENS
SOYBNS
surbis
LABOR 4
CAPSPLY1
CAPSPLY3
PERICD 3A
－1． 60
－1
.340 Lajulk
1．54U LABUK
． 230 CAPSPLY
－GIL CAPSPLY4
－47．600
$-12.050$
$-95.00 C$
LANDC
.680
LABUR 1
1.000
－270
860
.210
.790
－95．COC
－14．800
$-40.000$
LANDC
.46
.650
.16 C
4.500
－40．0ご0

$$
\begin{array}{r}
79.680 \\
1.000 \\
.530 \\
.610 \\
-61.290 \\
70.250 \\
1.000 \\
.530
\end{array}
$$

LABUR 1
.010
CAPSPLYZ
． 210
DL20
DL20
LL20
0L40
LL40
DL40
ANCC
LAECRZ
LABUR4
CAPSPLY3
RETURNS
LANDC
LABORZ

LABOR1
l． 800
.250
1.000
.200
BEANS
LABUR 2
CAPSPLYI
CAPSPLY3
PERICE＋A

LABOR 3
.780
.686
9.430
.710
1．6．0
$-10.390$
1．tU0
1．ucu
.010
.210

TABLE 24．（CUNTLNUEJ）．

| D L 40 | LABSCR4 | － 11 l | CAPSFLYZ | －15．030 |
| :---: | :---: | :---: | :---: | :---: |
| DL4 | CAPSPLY | －54．226 | RHSC | 1．0U6 |
| DL50 | KETURNS | 0 － 070 | L Aivoe | 1．uひ |
| リLち | LANIC | 1・しいし | LAburl | ．01i |
| CL5u | LABCRZ | ． 530 | LABUR 3 | ． 210 |
| ULS6 | LAELR4 | －Ulu | CAPSPLY2 | $-15.610$ |
| DL 5c | CAPSPLY3 | －52．5tic | RHSD | 1．じすく |
| CLSI | LANLA | －1．vしひ | LANDB | 1．LCC |
| CLSI | LANLC | 1．しこう |  | － |
| ClS 2 | LANDA | －1．66 | LANDC | 1．じく |
| CLS 2 | KHSA | 1 －ひひ |  | － |
| EUYCURN1 | REIUKNS | $-1.260$ |  |  |
| BUYCLRNI | CAPSPLY1 | i． 060 | Periudi | －1．U6i |
| BLYCCRN2 | KLTURNS | －1．190 |  |  |
| BUYCURN | CAPSPLYZ | 1．USU | PERIULZ | －L．cou |
| ELYCLRN3 | RETURNS | －1．170 |  |  |
| こUYCLKN3 | CAPSPL Y3 | 1．17し | PERILU3 | －1．000 |
| CUYCERN4 | RETURIS | －1．-4 |  |  |
| ELYCCRIN4 | CAPSPLY4 | 1． 40 | PEKICL4 | $-1.600$ |
| SELCURN1 | RETURNS | 1． $0<6$ |  |  |
| StLCCRML | CAPSPLYI | －1．026 | PERILUL1 | 1．Uno |
| SELCCRN1 | CLKNPRCD | 1．u60 |  |  |
| ScLelknz | RETURNS | 1.650 |  |  |
| SELCLRNZ | CAPSPLY 2 | －1．05u | PER1ULZ | 1．Lu |
| SELCLRN | CLRNPKLO | 1．LCu |  |  |
| SELCLRA3 | KETURNS | 1.130 |  |  |
| StLCLNN3 | CAPSPLY3 | －1．130 | PEくillu3 | 1 －ubu |
| SELCLRN3 | CURINPRUD | 1． 060 |  |  |
| SELCLRA4 | KETURAS | 1.000 |  |  |
| SELCURiv4 | CAPSPLY4 | －1．しごし | PLRICL4 4 | 1．030 |
| SELCCRA4 | しLKNPROL | 1．0UC |  |  |
| SELLCAT1． | RETURNS | .680 | CATGRN | 1．じ心 |
| SEllilati | CAPSPL Y | －．08C | PERIClia | 1．ひひひ |
| SELLLATZ | RETURNS | ． 7 C 0 | UATGRN | 1．しく0 |
| Seiluatz | CAPSPLY2 | －． 7 CL | PERICD2A | 1.000 |
| SELLCAT 3 | RETURNS | .64 C | UATGKN | 1．ごo |
| SELLLAT3 | CAPSPLY3 | －．040 | PERILL3A | 1． 100 |
| SELLUAT4 | KLTLRNS | ． 600 | CATGRN | i．vu0 |
| SELLLAT4 | CAPSPLY4 | －． 600 | PERIGD4a | 1．CuC |
| SELLSBSI | KLTURNS | 2.500 | BEANS | 1．0uc |
| SLLLSBS 1 | CAPSPLYI | －2．26 | Perivula | 1．じく |
| SLLLSose | KETURAS | 2．350 | BEANS | 1．0じ |
| S上LLots | LAP SPLYE． | $-2.550$ | pekicliza | 1．ひUU |
| SELLSBS | RLTURNS | 2.710 | BEANS | 1．UCO |
| SrLLSHS3 | LAPSPLY3 | $-2.110$ | Pekillua | 1・びく |
| SELLSoS4 | REIURNS | 2.4 Cu | BEANS | 1．ひU |
| SELLS3S4 | CAPSFLY4 | －2．400 | PERIUE4A | 1．じく |
| SELLHAYL | RETURNS | 9.050 | HAYL | 1．vuo |
| SELLH．AYL | CAPSPLV3 | －9．65C |  |  |

TABLE 24．（6LNTINULD）。

EUYHAYL

> ketukns

BLYHAYL
HUESI
HCGSI
HuGS 1
HuGSI
HOGS1
HUGSI
HCGS1
hugs 1
t．cuse
HCGS2
huGS2
HLGS 2
HUGS？
HUGS2
HEGSZ
HOGS2
h．ces 3
HCGS3
Hicgs 3
HCGS3
HUGS3
regs 3
HCES3
hoces
HLGS4
HGGS4
hicis 4
HLGS4
HGGS4
HCGS 4
HCGS4
HUGS4
FEcLERi
feEUCRI
FEEDER1
FEECEKI
FeEDER 1
FEEDER1
reEuerz
FEECLRL
FEEDERZ
FLEDLR2
rteDekz
FEEDLK
reveliks
1ELL゙Rく」
（CEDERう

CAPSPLY3 RETURNS
LAECR1
Laburs
LAGURS f EEUNAXI
CAPSPLY4 PEKILEL PERICD4 kETURNs LAELKL LADUK 3 LABCRJ fEEUNAXI CAPSPLYZ pericel PERIUD 4 RETURNS LABCR1 LABUR 3 LABCR＇S FELDMAX2 CAPSPLYE PERICDC PEKilld 4 returivs LAELRi LABOR 3 LAELRS FEEDMAX3 CAPSPLY4 PERICLZ PERIUD 4 RETURNS LADCKI LABUR5 FEELMAX4 CAPSPLY4 PERIUL4 RETURNS LABUR 1 Laclas fleináace CAFSPLYZ pepille जEIURNS LABCKZ LADER4

$$
\begin{array}{r}
-11.750 \\
10.750
\end{array}
$$

$$
26.65 C
$$

． 560 $\angle 3.220$
－buo
－2s．tid
4.850
.19
29.68 C
.770
． 56
． 5 b
.500
$-36.660$
4.35
.430 25.070
－らろし
． 88 C
.21
－300 $-21.400$
.190
4.85 c 15.206
.310
． 616
－ 500
11.010

4．8bc 12.420
－cel
． 316
1.06
$-20.020$
4.050

16．ちゃし
－ 86
－IL
.500 LABUK 2.510
LABCR4
.770
.880 CAPSPLY1－32．986
1．000 rizLMAX4－．5：0
6.330 PEKRLLD 4．056
.430 PEKLUL3 ．is
4.050 FARUNAX4 l．．．．
.080 LABURZ ．DCO
． 510 Lablka ． 550
．77C CAPSPLYi 6．3EC
bELLVAXZ
1．0vo
4.850

HAYL．
－1．い．
.430
1.000
.800
－うlu
0.280

1・ジu
． 196
4.850

1．ulo
.770
－jou
c． 330
1．．uc
.430
4.850

1．600
.060
$-26.890$
－
4.850

1．UL
.620
11.400
4.850
.50
.020
12.500

TAELE 24．（CUNTINULD）．

| JEELER3 | FEELMAX3 | 1． 660 |  | － |
| :---: | :---: | :---: | :---: | :---: |
| FEEUER3 | LAPSPLY3 | $-29.080$ | PLRIGUL | 4．cとこ |
| FELUER3 | PERILES | 4.856 | FLEDMAX2 | － 5 － |
| FEEDER 4 | KETURNS | 14．556 |  |  |
| FEEDER4 | LAECR3 | ． 860 | LABOR 4 | － 62 l |
| FEEDER4 | LADURS | ． 310 | CAPSPLY3 | 11．010 |
| FCECCK4 | Fcilmax4 | 1．006 |  | － |
| ftever 4 | CAPSPLY4 | －20．760 | Pekiuls | 4.000 |
| FEEDER4 |  | 4.25 | rllerivax3 | －らし |
| h上ANckl | KLTUKNS | 8.680 |  |  |
| atancri | LABLK1 | － 120 | LABLRZ | －1， |
| WEANEK1 | LAEORS | －＜uひ | LAOUK4 | － 550 |
| nEANER1 | LABLRS | .170 | CAPSPLYI | －7．0く́l |
| WC A AXLA 1 | FARUMAXI | 1．6uc |  | － |
| WEANEK1 | CAPSPLYE | －．820 | PEんIUご | －686 |
| WL ANERく | KETURINS | 8.45 C |  |  |
| WEANLRZ | LABGRI | .77 C | LABER2 | ． 120 |
| WEANEKZ | LABCR3 | －100 | LABUR 4 | － 200 |
| WEANER2 | LABURS | ． 550 | CAPSPLYC | $-7.700$ |
| WC ATVER2 | FARLMAX 2 | 1．0．u |  | ． |
| hEANEK2 | CAPSPLV3 | －． 750 | PERICL2 | ． 600 |
| WEANER3 | 良ETUKNS | 9．60し |  |  |
| WEANER3 | LAbCR1 | .550 | LABUR2 | ． 770 |
| W L ANER 3 | LAECK3 | .120 | LAUCR4 | －1uv |
| NEANER3 | LABOR | － 2 CC | Capsplyz | －c． 750 |
| heANERS | FARCNAX3 | 1．ひひす |  | － |
| wcantr． | CAPSPLY4 | －．ESC | Plizill3 | － 60 U |
| WEANER4 | REJURAS | 7.780 |  |  |
| WL－AMLR4 | LABLRL | ． 2 c 0 | LAELRE | －コらい |
| WEANLR4 | LAELR3 | ． 77 c | LABLR4 | － 120 |
| heanek 4 | LABLKう | ．100 | GAPSPLYL | －． 780 |
| WEANCR 4 | FARUMAX1 | 1．LVC |  |  |
| WEANLR4 | CAPSPLY4 | －7．000 | PERIUD4 | ． 080 |
| TURKEYS | RETUKNS | 33.130 | TURKLANE | － 33 |
| TURKEYS | LABUR 2 | ． 258 |  |  |
| TURKEYS | LABCR3 | ． 332 | LABUR 4 | －113 |
| TURKEYS | LABOR 5 | .117 | CAPSPLYZ | 7.270 |
| TURKEYS | CAPSPLY3 | $-16.570$ | CAPSPLY4 | $-23.030$ |
| TLRKEYS | PERICUZ | 1.150 | PEKICL3 | 3.67 v |
| TURKEYS | PERIOU4 | 4．53C | TURKMAX1 | 1.000 |
| HicgSexl | RETUKNS | 24.970 |  |  |
| HCGSEXI | LAECR1 | ． 500 | LABCR2 | .510 |
| HEGSEXI | LAEOR3 | ． 560 | LABUR 4 | .770 |
| H：GSEXI | LADCRS | ． 800 | CAPSPLYL | $-32.41 \mathrm{C}$ |
| HugSLXI | LAPSPLY4 | 7． 44 C | PER1Lbl | 4.850 |
| HuGSEXI |  | ． 430 | PLRIULS | .190 |
| Hicuse $\mathrm{Xl}_{1}$ | Ptinices | 4．8゙つ |  | － |
| Hegstx 2 | KLIUKNS | 21．54じ |  |  |
| HLGSLXK | LAELK1 | －bou | LADUK2 | － 300 |

TAELE 44 •（CONTINULU）．

| HLGJこX2 | LABLR | ． 210 | LAdCks | －らうし |
| :---: | :---: | :---: | :---: | :---: |
| hCGSEX2 | LAEORら | .776 | CAPSPLY | 7.45 |
| HCGSEX2 | CAPSPLYE | －＜y．uうu | Pckill | 4.050 |
| HUGSEX | PERICLZ | 4.05 | PENICU3 | ．430 |
| HLGSEXL | PERIOL ${ }^{\text {r }}$ | ． 140 |  | ， |
| HUGSt $\times 3$ | RETUKNS | 28. vus |  |  |
| HuGSEX3 | LABUR | .77 C | LABUR2 | － 380 |
| HCGSEX3 | LAELR3 | .500 | LABUR 4 | .310 |
| HUGSEXJ | LABCRS | － 550 | CAPSPLYC | 7.490 |
| HCGSEX3 | LAPSPLY3 | －32．490 | PEKIULI | －190 |
| HLGSEX3 | PEKICL2 | 4.350 | PLRICL3 | 4.350 |
| HUGSEX3 | PERIOD 4 | ． 436 |  | － |
| HCGSEX4 | RETURNS | 22.290 |  |  |
| HOGSEX4 | LADCR1 | .55 C | LABLR2 | .770 |
| HLGSEX4 | LABOR3 | ． 836 | LASOR 4 | －bol |
| HCGSEX4 | LAECK5 | ． 510 | CAPSPLY3 | 7.440 |
| HUGSEX4 | CAPSPLY4 | $-30.730$ | PEKICEL | －430 |
| HCGSEX4 | PERILOL | ． 190 | PLRICO3 | ＋．050 |
| Hussex4 | PERILU4 | 4.350 |  | － |
| Frediex 1 | RETURA．S | 14．67C |  |  |
| f LCELX | LABLRL | －310 | LADUK4 | ． 6.0 |
| Fravex | LABLR | －616 | CAPSPLY1 | －（0．7） |
| revilexi | CAPSPLY4 | 12．じい | Pckitul | 4.830 |
| ratelicxi | PEKICU4 | 4.1500 |  | － |
| Fetuex2． | HeTURAS | 11．0くて |  |  |
| Fetelx2 | LAECRL | ． 806 | LAUURく | － $0<2$ |
| Fredix 2 | LAbCR3 | ． 316 | CAPSPLYI | 11.0 bu |
| Ftelex 2 | LAPSPLY2 | $-22.67 C$ | PtikIUU 1 | 4.050 |
|  | PLRIUDZ | 4.850 |  | － |
| FEELLX3 | Labura | － 360 | LAOLR3 | －020 |
| FEELEX3 | RETURNS | 15.980 |  |  |
| FLeDexs | LASUR4 | ． 316 | CAPSPLY $\angle$ | 12.950 |
| FEEUEX3 | CAPSPLY3 | $-28.536$ | PLRIULZ | 4.850 |
| FEELEX3 | PERILUS | 4.850 |  | － |
| FEEOFX4 | RETURNS | 13.930 |  |  |
| FEECEX4 | LAEOR3 | ． 860 | LAUUR4 | － 626 |
| FELDEX4 | LABCRS | ． 310 | CAPSPLY 3 | 11.060 |
| FLCLEX4 | CAPSPLY4 | －25．816 | perilios | 4．8力 |
| FEEDCX4 | PERICD4 | 4.350 |  | － |
| WFANEX1 | Kr IURAS | 7－dしく |  |  |
| wLEAALXL | LABOK 1 | － $1<6$ | LADOR2 | －i心し |
| hi：AnLXL | LABCry | －LuO | LABCK4 | －コンし |
| wi．Aril Xi | LAbじから | ． 718 | CAPSPLYL | －1．02 |
| ni A小L $\mathrm{Cl}_{1}$ | CAFDPLY＜ | $-.130$ | PLKiUbl | －くごし |
| meaicke | KL IUKAS | 1．） 70 |  |  |
| h L ANLX | LABLRL | ． 17 | LASURC | －1吅 |
| Wi．AnLX2 | LABLRJ | －1uv | LAtuk 4 | ． 2 L |
| W上ANc X 2 | LADOR 5 | ． 556 | CAPSPLY $\angle$ | －7．48u |
| wEANEX2． | CAPSPLYS | －． 096 | PERIUL 2 | ． 080 |

1ABLE く4．（LUNTINLLD）．

| mLANEX3 | RETURNS | $8.72 u$ |  |  |
| :---: | :---: | :---: | :---: | :---: |
| WE．ANEX3 | LABUR 1 | ． 550 | LABCR2 | ． 77 |
| MLEANLX3 | LABUR3 | ． $1 \angle 0$ | LAEUR4 | －100 |
| ne Aivex 3 | LABCRS | －2uv | CAfSPLY； | －3．230 |
| heantx 3 | CAPSPLY4 | －． 190 | PERIUN3 | ． 080 |
| hEANLX4 | RETURNS | C． 96 |  |  |
| WEANEX4 | LABCK1 | － 2 CL | LABCR2 | －bbu |
| SLANEX4 | LAEOK 3 | ． 776 | LABUK4 | －120 |
| WEANEX4 | LAELRO | －1し） | CAPSFLYI | －．12C |
| AEANEX4 | LAPSPL Y4 | －6．78し | PERICじく | ． 080 |
| TUKKLX | RLTURNS | 22．16u | rukikl aives | － 433 |
| Tじにく， | LABCR 2 | －くゝコ |  |  |
| TURKEX | LABUR3 | ． 322 | LABCK4 | .113 |
| TUKKEX | LAELR5 | .117 | CAPSPLYZ | $8 .<40$ |
| TURKEX | CAP SPLYS | $-16.576$ | CAPSPLY4 | $-23.836$ |
| TURKEX | PLRICL2 | 1.150 | PERIOUZ | う． 070 |
| TCRKEX | PERICD4 | 4.330 | TUKK ${ }_{\text {I }}$ AXC | 1．uvo |
| CTR1 | CAPSPLYL | 1．じい | CAPSPLYZ | －1．Ulio |
| CTR2 | LAPSPLYZ | 1． 200 | CAPSPLY | －1．60心 |
| CTR3 | LAPSPLY3 | 1.600 | LAPSPLY4 | －1．0ひ |
| CTR4 | CAPSPLYL | $-1.000$ | GAPSPLY4 | 1．UCじ |
| FCPAL | LAPSPLYI | 1．${ }^{\text {duc }}$ | FCUSTS 1 | 1．6uし |
| FLPAL | LAPSPLYZ | 1．Cue | FGUSTSL | 1．くuo |
| FCPA3 | CAPSPLY3 | 1．6く | FCustsj | 1．0ひ6 |
| FCPA4 | CAPSPLY4 | 1．しひう | FCLSTJ4 | 1．ひひU |
| LENSIUK」 | PEK10uli | 1．lic | PERIOE2K | －1．L．${ }^{\text {c }}$ |
| CLNSIER1 | GSTKMAX1 | 1．000 |  | － |
| CENSIURZ | PLKIOU2L | 1．ひくご | PLKıOLJ | －1．vus |
| CLASILRE | GSIRMAX2 | 1．0゙0 |  | － |
| CLNSTOR 3 | HEKICDS | 1．0uc | PLR10L4 4 | －1．uve |
| CLINSTİR3 | GSTRMAX3 | 1．しん |  |  |
| CLASTLK4 | PERICDII | －1．000 | PERIUD44 | 1.000 |
| CUNSTER4 | GSTRMAX4 | 1．CuC |  | － |
| CRATRAN1 | PERIOU4 | －1．0co | PERICD 44 | 1.000 |
| CRATRANZ | PERICO3 | －1．0U0 | PERIUE33 | 1.000 |
| CRNTRAN 3 | Periouz | $-1 . C O C$ | PERI LD22 | 1． 100 |
| LKNTRAN4 | PERICUI | －1．cしo | PERIOD12 | 1． 0 Ce |
| BCNSTURI | PERICUI | 1.000 | PEH1LLZ | －1．000 |
| BCNSTUR1 | GSTRMAX1 | 1．v00 |  |  |
| BCASTERZ | PcRICD2 | 1． 000 | PtkIUDj | $-1.000$ |
| BGNSTOK2 | GSTRMAX1 | 1．JuO |  |  |
| BCNSIUR3 | PEKlCL3 | 1．び心 | PLRIOD 4 | －1．UC6 |
| HLNSTLR3 | GSTRMAXI | 1． |  |  |
| LCNSITH2 | PiRluita | －1．と．ご | PLR16L4 | 1．いい。 |
|  | G）RMAXL | 1．ひも |  |  |
| GKNSTLK1 | Pikillila | 1．ししく | PA，16LLA | －1．6こし |
| 6KNSILR1 | G）1RMAX1 | 1．Uし |  |  |
| uRhStc．e | PESIELZA | 1．ひひひ | PbkIUlja | －1．lud |
|  | GSTKMAXC＇ | 1．uct |  | － |

TABLE 24．（CCNTINULD）．

| GRNSTUR3 | PERIOLZA | 1． 000 | PLKIUL4A | －1．cuc |
| :---: | :---: | :---: | :---: | :---: |
| GKNSTCR3 | GSTRMAX3 | 1．vuy |  | － |
| GRNS TUR 4 | PERIUDIA | －1． 200 | PERILL4A | i．cue |
| ERNSTER4 | GSTRMAX4 | 1．しく0 |  | － |
| BUYGRNST | RETURNS | －． 056 | GSTKMAXI | －1．uvj |
| BUYGRNST | GSTRMAX2 | $-1.000$ | GSTRMAX3 | －1．000 |
| SUYGRNST | GSTRMAX4 | －1．000 | CAPSPLY1 | － 050 |
| CALF $1 \angle A$ | RETURNS | 111.930 | LANDC | －v04 |
| CALF12A | LURNS IL | 2．t32 |  |  |
| CALF 12A | LABCRI | 1.820 | LABCRE | 1． $2 C 0$ |
| CALF12A | LABUR3 | ． 550 | LABCR4 | －350 |
| CALFILA | LABCKS | $.1 \angle 0$ | CAPSPLYi | 135．750 |
| CALF12A | CAPSPLYZ | 23.220 | CAPSPLY3 | $-270.930$ |
| CALFILA | PERIGLI | 17．20C | PLRIUL2 | 1 2.0 UC |
| CALF12A | PERICDS | 10.400 | PLKIUU4 | 4．くOU |
| CALF22A | RETUKNS | 119.700 | LAADC | － 304 |
| CALF $22 A$ | CURNS IL | 1.020 |  |  |
| CALF $22 A$ | HAYL | .742 | LABCR1 | 1.820 |
| CALF22A | LABUR 2 | 1．2u0 | LAJUR3 | ． 955 |
| CALFく2A | LAECR4 | .350 | LABUR 5 | ． 12 C |
| CALF $22 A$ | CAPSPLYI | 120.500 | CAPSPLY2 | 19.440 |
| Calf 22A | CAPSPLY3 | －265．78 |  |  |
| CALF22A | PERICDI | 16.900 | Perille | 12.4 CC |
| CALF 22 A | PEKIUN3 | 16．30C | PERICL4 | 4.100 |
| YRLG32A | RETUKAS | 88.260 | LANDC | － 264 |
| YRLG3＜A | COKNSIL | 1.710 |  |  |
| YRLGこ2A | LABUR1 | $1.78{ }^{\circ}$ | LABUR2 | － 980 |
| YRLG3 2 A | LAECR5 | ． 140 | CAPSPLYE | 19．512 |
| YRLG32A | CAPSPLY | $-200.260$ | CAPSPLY4 | 130.490 |
| YKLUS2A | PLRIULI | 24.106 | PENILIL2 | 11.300 |
| YRLG32A | FER1しめ4 | 12.200 |  | － |
| YKLG42A | KETURNS | $9 \mathrm{C}$. | LANUC | －004 |
| YL．LG42A | CCRAS IL | 1.197 |  |  |
| YKLG4 2 A | HAYL | ． 294 | LAOUK1 | 1．70 |
| YRLG42A | LAELR2 | .980 | LABUR 5 | ． 144 |
| YRLG42A | CAPSPLYI | 9.890 | CAPSPLY2 | $-205.530$ |
| YKLG4 2 A | LAPSPLY4 | 165．11C |  |  |
| YRL642A | PERILEI | 22.200 | PERIULC | 16.200 |
| YRLG42A | PER1CU4 | 12．1v0 |  | － |
| STEER32A | REJURNS | 74．USC | LANUC | －Cer |
| STEER32A | CCKNSIL | 1．30り |  |  |
| STEER32A | LABUR 2 | ． 470 | LAuCR3 | 1．360 |
| STEEKっ2A | LABUR4 | 1．360 | LABUR5 | － 43 C |
| STELR32A | LAPSPLYZ | 168.190 | CAPSPLY3 | 130810 |
| STEER32．A | CAPSPLY4 | －2t1．－9C |  |  |
| STEER32A | PEKIUDZ | 1J．400 | PE，10：3 | 15．356 |
| STERS3くA | PERIUU4 | 6．3UC |  | ， |
| STLEK42A | RLTURiNs | 75.03 | LANOC | －U64 |
| STEİR42A | CCKASIL | .413 |  |  |

TABLE＜4．（CLNT INUEL）．

| STEER42A | HAYL |
| :---: | :---: |
| STEER42A | LABOR3 |
| STEER42A | LABURS |
| STEER42A | LAPSPLY3 |
| STEER42A | PERICDZ |
| STEER42A | PERICO 4 |
| BUTH3 2 A | KLTURNS |
| DCTH32A | CLRASIL |
| HOTH3 2 A | LAGOR1 |
| ELTH32 A | LAUORJ |
| BCTHELA | LABLK＇ |
| BUTH32A | CAPSPLY |
| BLIH32A | CAPSPLY4 |
| BUTH32A | PERICDZ |
| ELTH32A | PLRIUL4 |
| BLTH42A | RLTLRNS |
| BUTH42A | LURNSIL |
| ROTH42A | HAYL |
| BUTH4 $\angle \mathrm{A}$ | LABCR2 |
| ECTH42A | LABUR4 |
| BLTH42A | LAPSPLY1 |
| DUTH4 2 A | CAPSPLY3 |
| ELTH4LA | PERIOLI |
| BUTH42A | PERICD3 |
| CALF120 | RETURNS |
| CALF120 | CCRASIL |
| CALFLCO | LASLRI |
| CALF12B | LABOR， |
| CALFL2is | LAECR＇ |
| CALF125 | LAPSPLY2 |
| CAL 12 B | PLRIULI |
| CALF 123 | Prekicu 3 |
| CALF $22 B$ | RETUKNS |
| CALF223 | CLKASIL |
| CALF 228 | HAYL |
| CALFZ2E | LABUR2 |
| CALF223 | LASLR4 |
| CALF223 | CAPSPLY1 |
| CALF223 | CAPSPLY3 |
| CALF 228 | PERIOD 2 |
| CALF228 | PERIOD 4 |
| YRLG328 | RETLRNS |
| YRLG323 | CUKNSIL |
| YRLG32B | LABCRI |
| YRLG320 | LABCR5 |
| YKLG328 | CAPSPLYZ |
| YKLGつ2D | PLRICU1 |
| YRLC32d | PEKIUDA |
| YRLG42 ${ }^{\text {P }}$ | KETURNS |


| － 224 | LABLR2 | ． 47 J |
| :---: | :---: | :---: |
| 1.30 C | LABUR 4 | 1．300 |
| ． 430 | CAPSPLYZ | 160.19 C |
| 15．816 | CAPSPLY4 | －259．830 |
| 10.700 | PERIOUZ | 15.830 |
| 6． 500 |  | － |
| 171.31 C | LANDC | － 014 |
| 3.015 |  |  |
| 1.750 | LAbCRZ | 1.450 |
| 1.300 | LAbUR4 | 1．360 |
| ． 370 | CAPSPLYL | 19.210 |
| －58． Cl | CAPSPLYO | 17.310 |
| －101．006 | PERIULI | 24.100 |
| 21.706 | rericus | 19.550 |
| 18.500 |  |  |
| 175.330 | LANLC | － 004 |
| 2．11C |  |  |
| ． 518 | LABUK 1 | 1.78 C |
| 1.450 | LABCR3 | 1.30 V |
| 1.360 | LABCR | .570 |
| 9.390 | CAPSPLYZ | $-57.34 \mathrm{C}$ |
| 14.61 C | CAPSPLY4 | $-93.720$ |
| 22.200 | PERIUDz | 26．SCi |
| 19.830 | PERICD 4 | 18.600 |
| 111.440 | LANDC | － 004 |
| 2.032 |  |  |
| 1.820 | LABCFIC | 1.200 |
| ．55C | LABUR 4 | ． 350 |
| .120 | CAPSPLY1 | 130.730 |
| $\angle 4.2 \angle C$ | CAPSPLY3 | － 271.445 |
| 17．2し0 | PERIULZ | 12．0じ |
| 10.400 | PERICL4 | 4．260 |
| 119．270 | LANLS | －U心4 |
| 1.020 |  |  |
| ． 742 | LABLK1 | 1．82v |
| 1.200 | LABLR 3 | ． 550 |
| ． 350 | LABLR5 | ． 120 |
| $1<6.560$ | CAPSPLY2 | 20.440 |
| $-266.270$ | PERIUDI | 16.500 |
| 12.400 | PERIUL3 | 13.300 |
| 4.100 |  |  |
| 07.750 | LANDC | －Uび |
| 1.71 C |  |  |
| 1.78 C | LABORZ | － 986 |
| ． 140 | CAPSPLYL | 1）．うこ0 |
| －205．756 | CAPSPLY4 | 158．4yし |
| 24.100 | PERIUDL | 11．36\％ |
| 12．2l． |  |  |
| 9 l .02 l | LANUC | － 64 |

TABLE 24．（CUNTINULU）．

| YRLG428 | CLKNSIL | 1.197 |  |  |
| :---: | :---: | :---: | :---: | :---: |
| YRLG420 | HAYL | ． 294 | LABCR1 | 1.780 |
| YRLG42B | LAECRZ | ． 988 | LABUK | 140 |
| YRLG42B | CAPSPLYI | 15.516 | CAPSPLYZ | －204．020 |
| YRiLG42B | CAPSPLY4 | 158．45C | PERIUU 1 | 22．2uv |
| YRLG423 | PERICLC | 10.200 | PERIOL4 | 12．100 |
| STEER323 | RETURNS | 73.570 | LANLC | － 004 |
| STELR32E | CLIKNS IL | 1.305 |  |  |
| STEER 32 B | LABCK2 | ． 470 | LAdCK3 | 1.360 |
| STEER3 2 B | LABUR4 | 1．36C | LABUR 5 | －43u |
| STEEKS2B | CAFSPLY2 | 168.190 | CAPSPLY3 | 15．810 |
| STEER323 | CAPSPLY4 | $-257.57 \mathrm{C}$ | PERICDL | 10．400 |
| STEER32E | PERIOLS | 19.55 C | PERICD 4 | 6.300 |
| STEER42E | RETURNS | 75.320 | LANLC | －004 |
| STEER42B | Curnsil |  |  |  |
| STEER42E | HAYL | ． 224 | LABURZ | ． 470 |
| STEEK423 | LAOCR3 | 1.360 | LABOR4 | 1.360 |
| STEER4 2 B | LABUK | ． 430 | CAPSPLYC | 160.190 |
| STEER42E | CAPSPLY3 | 14.310 | CAPSPLY4 | $-258.320$ |
| STEER42B | PERILOZ | 16.700 | PLRILUS | 19.830 |
| STEEK4 2 E | PERIUU4 | b．buc |  |  |
| BUTH323 | KETURNS | 171．60 | LANLC | 34 |
| BL Th323 | CORNSIL | 3.615 |  |  |
| BCTH3LE | LAELR1 | 1.700 | Labluk 2 | $1.45 v$ |
| ©UTH＝23 | LAOLR3 | 1.300 | LABCR4 | 1.300 |
| LんT $\mathrm{H}=\angle \mathrm{B}$ | LAbUKり | ． 576 | CAPSPLY1 | 14.550 |
| BLTH328 | GAPSHLYC | －97．600 | CAPDPLYO | 12.010 |
| טUTHZ2D | CAPSPLY4 | －99．030 | PERICDI | 24.100 |
| BCTH328 | PLRIOUZ | 21.700 | PERIUL3 | 15．こらし |
| BuTh323 | PLKICU4 | 18.500 |  |  |
| BUTH423 | RETURNS | 175．C8C | LANUC | －U 4 |
| BL．TH42is | CURASIL | 2.110 |  |  |
| 3OTH42B | HAYL | .518 | LABLR1 | 1.700 |
| BCTH428 | LABOR2 | 1.450 | LABUR 3 | 1.360 |
| 3CTH428 | LABCR4 | 1.360 | LADURS | － 57 C |
| bUTH423 | CAP SPLYI | 15.516 | CAPSPLYZ | －95．830 |
| ECTH428 | CAPSPLY3 | 14.810 | CAPSPLY4 | －95．830 |
| OLTH42B | PEKILD， | 15.830 | PERIUL4 | 1ó．uv0 |
| SUTH423 | PLKiUU1 | ご2．2しO | Pchilu）2 | 2u．sue |
| ＜L SHT HANL S | ILJS |  |  |  |
| Bij 1 | LANLG | 1920.06 | RHSA | 192u．uvo |
| © 1 | LABCK1 | 1ase． | LAJUñ2 | 115 くしして |
| いし 1 | LAbCK3 | 1u5\％．．lou | LABUR4 | $1 \ll 4 \cdot 0$ |
| 以し1 | LABUKう | 216 C ． CO | GSTRMAXI | 7しひしく。ひひくす。 |
| Bul | CSIRMAX2 | 7uひひu・ひu发 | GSIKMAX3 | フじくく．ひび |
| Bし1 | GSTRMAX4 | 760して。しひ0 | TUKKMAX1 | Ijuveuso |
| せU1 | TURKMAX 2 | $3660.6 し く$ | FARUMAXI | 勺しlelul |
| BCl | FARLMAX2 | 500.000 | FARCMAX 3 | 560.000 |
| BC 1 | FARUMAX 4 | $500 . C 00$ | FEEDMAXI | 420.000 |

TABLE 24．（CLNTINLEL）。

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de 2
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Ev2
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BU3
BC 3
BC3
003
せも3
BCS
Eu3
DC3
LO3
Eしs
LC． 3
2 C 3
BC4
BC4
Bu4
－ 04
BU4 GSTKMAX2
BU4 GSTRMAX4
BU4 TURKMIAXZ
E04 FAROMAXL
BC4 FARLMAX4
Bu 4 FEEDMAX2
BO4 FELEMAX4
Bし4 FGUSTSI
HO4 FCOSTS3
BUS
BC 5
RU5
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Bいう

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LABLRJ
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IURKMAXC
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FELLMAXく
Fecemax 4
FCOSTSI
rCOSTS 3
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LAECR3
LABCR5
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GSTKMAXZ
TURKMAXZ
FARLMAXZ
FARLNAX4
FELLMAXZ
FLEEMAX4
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|  | $2160 . L C 6$ |
|  | 2760.606 |
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|  | 2160.00 |
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| GSTRMAX 1 | 70ひび・し |
| TURKMAXI | 136ご。し |
| GSTRMAX 3 | 70ごく。じく |
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| FELDMAX1 | 420 |
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| cu5 | FAKUMAX2 |
| BC5 | FAKLMAX4 |
| BC5 | FEEDMA 2 |
| BC5 | FELLMAX4 |
| BC5 | FCCSTS1 |
| Bus | FCGSTS 3 |
| BU6 | LANDE |
| らしも | LABUR 1 |
| B6O | LABUR3 |
| 306 | LABCRS |
| いくも | GSTRMAX2 |
| 8u6 | ESTRMAX 4 |
| BC6 | TLKKMAXL |
| 006 | ＋ARCMAXE |
| らし6 | FARLMAX4 |
| くいく | Flelimax 2 |
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| Bu7 | LALLKl |
| Bu7 | LABLR3 |
| EC7 | LAUCR5 |
| BC7 | GSTRMAX2 |
| Bu7 | GSTRMAX4 |
| BC7 | TUKKMAXく |
| むu7 | FARUMAX2 |
| \＆u7 | FARLMAX4 |
| とC7 | FEELMAX $\angle$ |
| Eu7 | FECEMAX4 |
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| らしく | GSIKMAX2 |
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| としむ | FARUMAX 2 |
| ビ〕 | FELCMAX2 |
| 1368 | FARLMAX4 |
| BUB | FEELMAX4 |
| BCC | HCLSTSL |
| Bし8 | FCOSTS3 |
| Eu9 | LANDC |
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| GSTRMAX 1 | 7くししく・じす |
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| FEtUMAX 1 | 4くじいい |
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| GSTRMAXS |  |
| TURKMAXI | 13じ。じく |
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| B 12 | FGUSTS |
| Ely | LANEB |
| 13．3 | LANLl |
| B1） | LADURl |
| H13 | LARCR3 |
| B13 | LABLR5 |
| B13 | GSTRMAX2 |
| B13 | GSTRMAX4 |
| H13 | TURKMA $\times 2$ |
| 813 | FAREMAX 2 |
| －13 | FARCMAX4 |
| 1313 | FELDMAX $\angle$ |
| E1 13 | FELDNAX4 |
| E13 | FCLSTSI |
| B13 | FCUSTS？ |
| 814 | LAALE |
| 314 | LAINDC |
| 134 | LABUR 1 |
| 1314 | LABCK3 |
| B14 | LABUR5 |
| B14 | GSTRMAXZ |
| 614 | GSTKMAX 4 |
| E14 | 1 URKMAX2 |
| E14 | FARLNAXZ |
| E14 | FARLMAX4 |
| B14 | FELLMAX2 |
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[^0]:    ${ }^{1}$ This may not be a farmer's only objective, as explained on page 2.

[^1]:    ${ }^{1}$ The Layman reader is more likely to understand the term 'net protit' while the economist may prefer the concept of 'entrepreneurship return' as defined here.
    ${ }^{2}$ Operating costs include remuneration of labor and management.

[^2]:    ${ }^{1}$ This connection became apparent to the economists who took part in the development of linear programming. For example see Koopmans (32) and Dorfman (11).

[^3]:    ${ }^{1}$ For a discussion on the respectability of the assumption of constant returns to scale see Samuelson (35, p. 84).

[^4]:    ${ }^{1}$ For example see Candler and Musgrave (6).
    2 See R. E. Gomory $(16,17)$.

[^5]:    ${ }^{1}$ The possibility of labor merely drawing living expenses over three periods and receiving a large lump sum payment in the fourth period was considered. With the exception of small changes in the capital 'flows' the optimized plan remained unchanged. We therefore chose to allocate salaries in four even portions since the operators, like many people, are making time payments on various household items and thus prefer an even flow of income.

[^6]:    ${ }^{1}$ Although a five percent interest rate seemed reasonable when this study was initiated, recent increases in the cost of credit have rendered this figure on the low side.

[^7]:    ${ }^{1}$ Personal communication with the farm-firm operator.

[^8]:    Annual repair costs calculated at $3 \%$ of replacement cost.

[^9]:    ${ }^{\text {a }}$ Source: Table 4 and (41).

[^10]:    ${ }^{\text {a }}$ Source: Farm accounts and records, and (4).

[^11]:    ${ }^{\text {a }}$ Source: farm accounts and records, and (4).

